Errata: An Introduction to Stochastic Dynamics Cambridge University Press

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Chapter 2

- P30, line 2: $\mathbb{E} ||X_n X||^p$
- P30, bottom: missing the conditions: p > 1, q > 1, and $\frac{1}{p} + \frac{1}{q} = 1$
- P31, line 5: $\sigma > 0$
- P31, line 18: $M^k(0)$
- P36, lines 19, 20, 23, 24 and 27: $\mathcal{B}(0,T) \times \mathcal{F}; (0,T) \times \Omega$
- P36, line 20: change \mathcal{F} to $\mathcal{B}(0,T)$; change $\mathcal{B}(0,T)$ to \mathcal{F}

Chapter 3

- P51, line -5: Move $\frac{1}{\Delta t}$ to the left side
- P55, line 11: delete extra $\int_0^{+\infty}$

Chapter 4

- P65, line 8: delete extra s of $\tau_i s$
- P65, line 15: missing subscript i in τ_i
- P67, line -6: The integrand after the limit should be $f_n(t,\omega)$
- P67, line 10: change ms. to m.s. (missing dot in ms.)
- P67, line 22, at the first line of formula (4.8): change $\int_{T_0}^{T_f} f(t_i^n, \omega) dB_t$ to $\int_{T_0}^{T_f} \sum_{i=0}^{n-1} f(t_i^n, \omega) I_{[t_i^n, t_{i+1}^n)} dB_t$
- P78, line -9: delete extra s of fs
- P79, line 18, the first sentence in Example 4.13: change X^2 to X_t^2
- P86, line 8, at the end of (4.82): Delete the extra ')'.
- P88, line -3: change $f : \mathbb{R}^d \to \mathbb{R}^d$ to $f : \mathbb{R}^n \to \mathbb{R}^d$
- P89, line 1: change $f : \mathbb{R}^d \to \mathbb{R}^d$ to $f : \mathbb{R}^n \to \mathbb{R}^d$
- P89, line 3 (twice), the right hand: $x \in \mathbb{R}^n$
- P89, line 3: the second term in the right hand side should be double bar $\|\ldots\|$
- P91, lines 15 and 17: in line 15 'Ito SDE system' is different from 'Stratonovich SDE' in line 17. Why? Any difference between 'Ito SDE system' and 'Stratonovich SDE'?
- P96, line -4: change '?' to '.'

Chapter 5

- P113, line 4: change 'ridges' to 'ridge'
- P116, line 4: change X_t to X(t)
- P123, line 15, between (5.81) and (5.82): \mathbb{R}^n
- P126, line 10, Example 5.22: change W_t to B_t
- P129, line 15, Problem 5.1: change W_t to B_t , and change W_s to B_s

- P130, line 2: Problem 5.3: change linear to nonlinear
- P131, line 3: Problem 5.8: change W_t to B_t
- P131, line 13,17: Problem 5.9: change D = (-1, 2) to D = (1, 2)

Chapter 6

- P135, line 9, Eqn (6.3): $\phi_0(x_0) = x_0$
- P137, line 2: should be (6.6)
- P153, line 2: should be (t, ω)
- P156, line -3: $\mathbb{B}_{\tau}(\omega)$
- P158, line 16: change f to k
- P159, line 9: Eqn (6.62): should be $\mathbb{B}_s(\omega)$
- P160, line 5, Eqn (6.67) top: should be x^2
- P160, line 8: Eqn (6.68) inside parenthesis but before the integral sign: missing '2'.
- P172, line 19: change \mathbf{F} to $\mathbf{F}(t)$
- P175, line 7: ξ_t should be ξ
- P179, line 6, Eqn (6.125): should be (ω, x^s)
- P179, line 9, the left hand side of Eqn (6.126): (ω, x^s)
- P179, line 12, the right hand side of Eqn (6.127): (ω, x^u)
- P179, line 15, the left hand side of Eqn (6.128): (ω, x^u)
- P185, line -3: change '?' to '.'

Chapter 7

- P191, lines 10 and 12: change 'cadlag' to 'càdlàg'
- P192, line 6: change 'cadlag ' to 'càdlàg '
- P192, line -8, add: Recall that \mathbf{L}_t has a *càdlàg* modification on Ω_0 and $\mathbb{P}(\Omega_0) = 1$ (see David Applebaum book P88)

- P198, lines -5 and -9, (i) and (iii): change σ to σ^{α} (See David Applebaum book P35)
- P198, line -3: change $\frac{1}{2}\sigma^2$ to σ^2 (In fact, $\alpha = 2$, i.e. \mathbf{L}_2 corresponds to $\mathcal{N}(0,2)$)
- P199, line 5: change $\frac{1}{2}\sigma^2$ to σ^2

P.S. We can also change $2\sigma^2$ to σ^2 in P199 line -4 and P200 line 4, cause we need to unify the notations of Brownian motion i.e. \mathbf{L}_2 in chapter 7.

- P204, line 17: change $\frac{1}{2}\sigma^2$ to σ^2
- P202, Eqn (7.21), line 4 : change (2k)! to 2k!
- P203, line 10: missing c_{α} in three places
- P208, Eqn (7.36): change $-\check{\mathbf{L}}_{-t}^{\alpha}$ to $-\check{\mathbf{L}}_{-t_{-}}^{\alpha}$ (Adding the left limit for $-\check{\mathbf{L}}_{-t_{+}}^{\alpha}$, we will ensure the bidirectional Lévy process is left continuous with right limit.)
- P209 Remark 7.20, lines 3 and 4 : missing c_{α} in three places
- P209 Remark 7.20: The jumps are countable but dense in every time interval. Why? Is the dense true for one path of a sample ω or the pathes of union of ω set? Could we have a clear statement?
- P212, Fig 7.10: change C to c
- P213, Eqns (7.45) and (7.48): change $\theta_{\alpha,n}$ into -1
- P215, Eqns (7.54), (7.55) and (7.56): change g to $g(t, \omega)$
- P216, Eqns (7.57): change $X_{t_{-}}$ to X_t in two place. (Suggestion: we could change $X_{t_{-}}dt$ and $X_{t_{-}}dB_t$ to X_tdt and X_tdB_t , respectively, for SDE with Lévy noise in Section 7.4.2)
- P217, line 6: change 'cadlag' to 'càdlàg'
- P217, Theorem 7.26: delete 'Moreover, if Eqn (7.63)'
- P217, Theorem 7.26: Modify the proof for the Theorem, because the Picard iteration can not be applied for large jumps.
- P218, lines 5, 7 and -6: change $X_{t-}dt$ and $X_{t-}dB_t$ to X_tdt and X_tdB_t , respectively, to unify the notations with the suggestion given in P216, Eqns (7.57).

- P219, lines 1 and -3: change $X_{t_{-}}dt$ and $X_{t_{-}}dB_{t}$ into $X_{t}dt$ and $X_{t}dB_{t}$
- P220, line 1, and P221, line 3: change $X_{t_{-}}dt$ and $X_{t_{-}}dB_t$ to X_tdt and X_tdB_t , respectively
- P220, Eqn (7.67), line 1: The last term of the integral, should be $\sum_{i=1}^{n} y_i \partial_i g(x)$
- P221, line 9: ||y|| < 1
- P221, Eqn (7.71): $\|\xi\|^2$
- P221, Hypothesis (iii): delete 'Assume that there ...and additionally'. (In fact this statement is true for all Lévy processes.)
- P221, line -5: change [145,Lemma 19.21,p328] to [145,Lemma 17.21,p328]
- P227, Eqn (7.86): where $\theta_{\alpha,1} = -1$
- P229, Fig 7.24 line 2: change ' $\epsilon = 0.1$: d = 0.1' into ' $\epsilon = 0.1, d = 0.1$ '
- P233, Eqn (7.96): change |y| < 1 into ||y|| < 1
- P236, line -11: change x > 0.5 to x > -0.5
- P236, line -12: change P(x) to p(x)
- P237, Fig 7.29 line 1: change P(X) to p(x)
- P239, Eqn (7.107): change φ to v
- P239, Eqn (7.109): change p(x) into p(x, t) in the first term of the right hand.
- P239, Eqn (7.110): change $f(X_{t_{-}})dt$ into $f(X_t)dt$
- P239, line -4: delete extra ')' in the first term $f(x)p_x(x,t)$ ' of the right hand side.
- P240, lines 2, 6 and 10: $\theta_{\alpha,1} = -1$
- P240, Eqn (7.114): change $f(X_{t_{-}})dt$ and $\sigma(X_{t_{-}})dBt$ to $f(X_t)dt$ and $\sigma(X_t)dBt$, respectively

Hints and Solutions

• P257, Problem 4.2: change 'As explained in Section 4.1' to 'As explained in Section 4.4' in line 2.