Chapter 2: HF and High Data-Rate Systems

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Outline

- Wireless and wireline systems
- Modulation schemes
- Transceiver architectures
- Transceiver specification
- Link budget
- Phased Arrays
- Radar and radiometers

Radio Transceiver Example



16-QAM Fiberoptic Transceiver Example



110-Gb/s DP-QPSK Fiberoptic Transceiver



Electronic circuits: wireless vs. fiberoptic communications systems



SYNTHESIZER PLL

Radio vs. Broadband Fiber Circuits

- Input/Output vs. Output return loss (S params)
- Receiver Sensitivity @ BER and SNR (Q)
- Linear LNA vs. linear TIA
- NF vs. equivalent input noise current
- (Non)Linear PA vs. Non-Linear TX drivers
- P_o (average) vs. V_o (p-p)
- Frequency conversion vs. MUX/DeMUX

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Modulation Schemes

Information modulates carrier



- Modulation schemes
 - Analog
 - Digital
- Digital preferred because of
 - Robustness to noise, interference, fading
 - Ease of error correction and encryption

Digital Modulation Schemes



Amplitude Shift Keying or On-Off Keying =OOK

Frequency Shift Keying

Phase Shift Keying

Binary data encoding formats



Spectral content of RZ and NRZ encoded binary data



M-ary PSK and QAM

M-ary PSK has constant amplitude

$$s_i(t) = A \cos(\omega_0 t + \phi_i)$$

where

$$\phi_i = 2\pi \frac{i}{M}$$

for i=0,1,2 ...M-1, M = 2^{n} and *n* is the number of bits per symbol.

• M-ary QAM $s_k(t) = a_k cos(\omega_0 t) + b_k sin(\omega_0 t)$

Ex. 64QAM

$$(a_k, b_k) = \left((-1)^{d_0} \frac{1 + 2d_2 + 4d_4}{7}, (-1)^{d_1} \frac{1 + 2d_3 + 4d_5}{7} \right)$$

M-ary PSK, QAM Constellations



M-ary PSK, QAM

- Generation
 - By up-conversion
 - By direct modulation
- Detection: coherent only
- QAM modulation systems need very linear power amplifiers



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Transmitter Architectures

- The transmitter generates the modulated carrier signal
- Key components
 - carrier synthesizer
 - modulator,
 - power amplifier (PA)
- Modulation of carrier
 - by upconversion (linear)
 - directly, in amplitude, frequency, phase or pulse-width
- Direct modulation can be linear or non-linear (RF-DAC)

Direct Upconversion Transmitter



- An RF filter (not shown) must be placed before PA
- a_1 and b_0 are analog baseband signals
- LO frequency pulling by PA => need lots of buffering between LO and PA

Single-Sideband, 2-step Upconversion

- Most common
- LO pulling is relieved
- Additional IF filtering
- Stringent
 Ilnearity specs



$$s_{IF}(t) = (a_{I} + j b_{Q})e^{-j\omega_{IF}t} = a_{I}\cos(\omega_{IF}t) + b_{Q}\sin(\omega_{IF}t)$$

$$s(t) = [a_{I}\cos(\omega_{IF}t) + b_{Q}\sin(\omega_{IF}t)]\cos(\omega_{LO2}t) = \frac{a_{I}}{2}\cos(\omega_{RF}t) + \frac{b_{Q}}{2}\sin(\omega_{RF}t)$$

$$\frac{+a_{I}}{2}\cos[(\omega_{LO2} + \omega_{IF})t] + \frac{b_{Q}}{2}\sin[(\omega_{LO2} + \omega_{IF})t]$$

Direct Modulation Transmitter



Receiver Architectures

- Tuned homodyne receiver (also known as a direct detection receiver) (Earliest)
- (Super) Heterodyne receiver (Reginald Aubrey Fessenden, 1906, Brant Rock Massachusetts)
- Direct Conversion (Zero-IF) Receiver

Direct Detection Receivers

- Simplest, no VCO/PLL
- Large gain (>50dB) RF
 tuned amplifier => unstable
- Tunable RF filters difficult to integrate

$$[A_{V}s(t)]^{2} = A_{V}^{2}A(t)^{2}\cos^{2}(\omega_{RF}t) = \frac{A_{V}^{2}A(t)^{2}}{2}$$

 A_v = receiver voltage gain

- Digital: Bandpass $\Delta\Sigma$
 - * power hungry
 - needs VCO

$$s(t) = A(t) cos(\omega_{RF}t)$$



Superheterodyne Receivers

$$s(t) = A(t) cos[\omega_{RF}t + \alpha(t)]$$

- Single step
- Two step
 - robust,
 - many filters, difficult to integrate in IC



$$f_{RF} = f_{LO} - f_{IF}$$
 or $f_{RF} = f_{LO} + f_{IF}$

$$\begin{split} s_{\rm IF}(t) = &A(t) \cos[\omega_{\rm RF}t + \alpha(t)] \cos(\omega_{\rm LO}t) = > \\ &\frac{A(t)}{2} \cos[\omega_{\rm IF}t - \alpha(t)] \end{split}$$

Image Rejection Superheterodyne Receivers



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Direct Conversion (0-IF) Receivers



- Simple & easy to integrate
- LO leakage, pulling, self-mixing
- Sensitivity to 1/f noise, even order non-linearity
 - Noise figure degradation in monostatic radar

X



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Transceiver Specification

- Receiver specification
 - Frequency, gain
 - Dynamic range
 - Noise figure, noise temperature, sensitivity
 - Linearity
 - PLL phase noise
- Transmitter specification
 - Output power
 - Error Vector Magnitude (EVM)
 - Power Spectral Density (PSD) mask, or ACPR
 - Noise

Fundamental Limitations of Dynamic Range



Noise

Determines the threshold for minimum signal detection.

Noise can be introduced in receiver in two ways

- From the *external* environment through antenna or signal source impedance
- By *internal* generation in receiver's own circuitry

Common Types of Noise Generated in Circuits

- Thermal noise $kT\Delta f$.
 - caused by the random vibration and motion of carriers due to *T*.
 - its spectral density kT is constant up to at least 100 GHz.
- *Shot noise* occurs in active devices
 - due to quantum, random nature of carriers crossing potential barriers.
 - Its spectral density 2ql is constant up to high frequencies
- Flicker noise occurs in active devices and sometimes in resistors, and its spectral density follows the 1/f law.

Available Noise Power

- Is the power that can be transferred from a noise source to a *conjugately-matched load*, whose temperature is 0 °K, and thus *unable to reflect* back noise power.
- Although counter-intuitive, the available noise power from a device/circuit/body/antenna does not depend on its size. $-\frac{1}{2}$

$$\mathsf{P}_{\text{available}} = \frac{\overline{\mathsf{v}_{\mathsf{n}}^2}}{4\mathsf{R}} = \frac{4\mathsf{k}\mathsf{T}\mathsf{R}\,\Delta\,\mathsf{f}}{4\mathsf{R}} = \mathsf{k}\mathsf{T}\,\Delta\,\mathsf{f}$$

T may be

- 290 °K (terrestrial antenna)
- 30 .. 50 °K (satellite antenna)
- > 290 °K for noise diode or PIN diode (signal and noise source impedance are not equal)

2-Port Noise Factor, Noise Figure

$$F = \frac{SNR_{i}}{SNR_{o}} = \frac{SNR_{i}}{\frac{GP_{i}}{N_{a} + GN_{i}}} = 1 + \frac{N_{a}}{GN_{i}}$$
 NF=10log₁₀F

F is the degradation of the signal-to-noise ratio as the signal passes through the two-port.

G is the power gain of the two-port

*N*_{*i*} is the input noise power (usually the noise floor)

available from the antenna

 P_{i} is the input signal power

 N_a is the noise power added by the two-port

Two-Port Noise Temperature

$$N_i = k T \Delta f$$
 $T_a = \frac{N_a}{k G \Delta f}$ $F = 1 + \frac{T_a}{T}$ $(F-1) \times T = T_a$

• T_{a} is the equivalent noise temperature of the 2-port.

- *T* is the ambient temperature of the signal source
- The noise figure is a function of the ambient temperature.
 Noise figure measurements must specify the ambient temperature at which the measurement occurred.

Friis' Cascaded Noise Factor/Temperature

$$\mathsf{F}=\mathsf{F}_1+\frac{\mathsf{F}_2-1}{\mathsf{Ga}_1}+\ldots+\frac{\mathsf{F}_n-1}{\mathsf{Ga}_1\times\mathsf{Ga}_2\times\ldots\mathsf{Ga}_{n-1}}$$

$$T_{a} = T_{a1} + \frac{T_{a2}}{Ga_{1}} + \dots + \frac{T_{an}}{Ga_{1} \times Ga_{2} \times \dots Ga_{n-1}}$$

How do we derive it?



$$M = noise measure$$



Receiver Noise Floor and Sensitivity

 Noise floor defined at the output of the receiver, before the decision circuit or demodulator

Noise floor $=kT \Delta f G F$

G= overall gain of the receiver gain

F = receiver noise factor

- Receiver *sensitivity*, *S*_{*i*},
 - specified for a certain bit error rate
 - depends on the receiver $F(T_a)$ and required SNR_{RX} of the detector

 $\mathbf{S}_{i} = \mathbf{F} \cdot \mathbf{SNR}_{RX} \cdot \mathbf{k} \cdot \mathbf{T} \cdot \Delta \mathbf{f} = \left(1 + \frac{\mathbf{T}_{a}}{\mathbf{T}}\right) \mathbf{SNR}_{RX} \cdot \mathbf{k} \cdot \mathbf{T} \cdot \Delta \mathbf{f}$

Link Between BER and SNR

$$BER = \frac{1}{\sqrt{2\pi}} \frac{\exp\left[-\left(\frac{E_b}{N_o}\right)^2/2\right]}{\frac{E_b}{N_o}} = SNR \frac{B_n}{R_b}$$

- E_{b} is the bit energy
- *N_o* is the one-sided noise power density
- B_n is the noise bandwidth: $\pi\Delta f/2$
- R_{b} is the data rate


SNR vs. Modulation Scheme

Modulation	Efficiency*	SNR@BER=10 ⁻⁶
OOK-NRZ	1.0 (1) bits	13 dB
4L FSK	1.5 (2) bits	17 dB
QPSK	1.6 (2) bits	14 dB
8PSK	2.5 (3) bits	19 dB
16QAM	3.2 (4) bits	21 dB
64QAM	5.0 (6) bits	27 dB

*)Bandwidth efficiency = data rate/bandwidth = (ideal)

 $\frac{\mathsf{R}_{\mathsf{b}}}{\varDelta \mathsf{f}}$

Receiver Sensitivity Examples

5-GHz Wireless LAN System

• NF = 6 dB, B=20 MHz, QPSK => SNR =14 dB $S_i(BER=1E-6)=-174 \text{ dBm }+6+10 \log \left(\frac{20 \text{ MHz}}{1 \text{ Hz}}\right)+14=-174+6+73+14=-81 \text{ dBm}$ 60-GHz, 1.5-Gb/s Wireless LAN System

• NF = 9 dB, B = 1 GHz, QPSK => SNR =14 dB

$$S_i(BER=1E-6) = -174 \text{ dBm} + 9 + 10 \log \left(\frac{1 \text{ GHz}}{1 \text{ Hz}}\right) + 14 = -174 + 9 + 90 + 14 = -61 \text{ dBm}$$

12-GHz, HDTV satellite receiver

T=30°K, NF=1dB, B=6MHz, 64QAM=>SNR=27dB

$$S_{i}(BER=1E-6) = -184 \text{ dBm} + 3.5 + 10 \log \left(\frac{6 \text{ MHz}}{1 \text{ Hz}}\right) + 27 = -184 + 3.5 + 68 + 27 = -85.5 \text{ dBm}$$

Equivalent Noise Current and Receiver Sensitivity in Fiber Systems

$$S_i = \frac{Qi_n^{rms}}{R}$$
 $BER \approx \frac{1}{\sqrt{2\pi}} \frac{exp[-Q^2/2]}{Q}$

- Q is the eye quality factor
- I^{rms} is the equivalent input noise current of the fiberoptic receiver
- *R* is the photodiode responsivity (A/W)
- There is a direct link between *Q* and the bit error rate BER





Linearity Figures of Merit



Linearity and Distortion

- The 1-dB compression point: P_{1dB}
- Third-order intercept point: *IIP3, OIP3*
- Second-order intercept point *IIP2* (critical in 0-IF receivers)
- Broadband measures of linearity
 - Total Harmonic Distortion (THD) = the sum of the powers of all the harmonics, except the fundamental

Equations for IIP_n and DR

• *IIP*_n can be obtained graphically using dB scales

$$IIP_{n} = \frac{nP_{i} - IM_{n}}{n-1}$$

Output dynamic range with respect to the *n*-th spur

$$DR_n = \left(1 - \frac{1}{n}\right)(IIP_n - IM_n)$$

 Spurious signals due to an interferer *I*, must be *C* dB below the sensitivity level (*C* = margin)

$$IM_n = S_i - C \implies IIP_n = \frac{nI - (S_i - C)}{n - 1}$$

Example of IIP3 spec derivation

•
$$I_1 = I_2 = -38 \text{ dBm}, S_i = -60 \text{ dBm}, C = 14 \text{ dB}, f_1 = 64 \text{ GHz},$$

 $f_2 = 62 \text{ GHz} => \text{IM3 at } 60 \text{ GHz}$
 $\text{IIP}_3 \ge \frac{3 \times (-38) - (-60 - 14)}{2} = \frac{-114 + 74}{2} = -20 \text{ dBm}$

 The most relaxed IIP3 requirement is in the absence of an interferer. Eg. in OFDM systems, the sub-carriers can interfere with each other:

 $I_1 = I_2 = -60 \text{ dBm}, S_1 = -60 \text{ dBm}, C = 40 \text{ dB}, f_1 = 60.005 \text{ GHz}, f_2 = 60.01 \text{ GHz} = > IM3 \text{ at } 60 \text{ GHz}$

$$IIP_{3} \ge \frac{3 \times (-60) - (-60 - 40)}{2} = -60 + \frac{40}{2} = -40 \, dBm$$

Linearity of a Chain Two-Ports



Ga_i is the available power gain of stage i (i.e. power gain when its input and output are conjugately matched to the impedance of the preceding and of the following stages.

Dynamic Range in Cascaded 2-Ports

Designing for maximum dynamic range:

- Make the noise level at the output of the first stage match that at the input of the second, third ... stages.
- Each stage contributes noise and distortion equally.



PLL Phase Noise: L

- L = a broadening of the oscillator spectrum
- Measured as noise power in dBc/Hz in a 1-Hz band at an offset frequency f_m relative to the carrier power and frequency f_{osc}



- Degrades the receiver sensitivity by raising the noise floor and adding *rms* phase error
- Degrades transmitter *EVM*
- Affects velocity resolution in automotive cruise control radar

Ex. of PLL Phase Noise Impact

 A phase noise of -100dBc/Hz over a bandwidth of 5 MHz results in a rms phase error

 $\theta_{\rm rms} \approx \sqrt{2 L \Delta f} = 0.0316 \, \rm rads = 1.81^{\circ}$

- Oscillator phase noise mixes with an undesired signal and is downconverted to the IF/baseband raising the noise floor and dictating how closely adjacent channels may be spaced
- Formula that gives maximum allowed phase noise to achieve adjacent channel rejection of C dB for an interference power I

 $L(f_m) = P(dBm) - C(dB) - I(dBm) - 10log(\Delta f), (dBc/Hz)$

In a 60-GHz radio with P=-60 dBm, C=14 dB, I=-38dBm, Δ f=2.1GHz,

Transmitter Specification

- *Output power* in dBm ($V_{pp}/50\Omega$) in fiber systems
- EVM = distortion in the transmitted signal constellation
 - measured with an ideal IQ receiver

$$EVM = \sqrt{\frac{1}{1000 \cdot P_{avg}}} \sum_{i=1}^{1000} \left[(I_i - I_i^*)^2 + (Q_i - Q_i^*)^2 \right]$$

 P_{avg} = average power of the constellation, (I_i^*, Q_i^*) are the complex coordinates of the ith measured symbol, and (I_i, Q_i) are the complex coordinates of the nearest constellation point.



Power Spectral Density Mask, ACPR

 PSD (eye mask in fiber) is specified in dB relative to the signal power in the center of the channel to prevent unwanted emissions into adjacent channels



- Adjacent Channel Power Ratio (ACPR) is another parameter specified in dB: 10log10.
 - Ex: <-20 dBc for 16 QAM, <-43 dB for 64 QAM

Transmitter noise

- *Transmitter noise (jitter),* mostly from PLL, degrades EVM.
- In fiberoptic transmitters the maximum allowed jitter of the output eye is specified





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Link Budget. LB

 Describes the combined transmitter, antenna, and receiver performance

$$LB = P_{RX} - S_{i} \qquad P_{RX}(d) = P_{TX}G_{TX}G_{RX}\left(\frac{\lambda}{4 \pi d}\right)^{2}$$

- λ is the wavelength
- *d* is the distance between the TX and RX $>>\lambda$
- P_{RX} is the power at the receiver input
- P_{TX} is the power at the transmitter output
- G_{TX} is the gain of the TX antenna (dBi)
- G_{RX} is the gain of the RX antenna (dBi)
- $EIRP = P_{TX}G_{TX}$ effective isotropic radiated power (*dBmi*)

Example: 60-GHz Link Budget

- 2-m 60-GHz link at 4 Gb/s with Δf of 2 GHz
- QPSK modulation, SNR = 14 dB, NF = 7 dB

 $S_i = -174 dBm + 10 log_{10} (2 \times 10^9) + 7 dB + 14 dB = -174 + 93 + 7 + 14 = -60 dBm$

•
$$P_{TX} = 10 \text{ dBm}, G_{TX} = G_{RX} = 8 \text{ dBi}, \lambda = 5 \text{ mm}$$

$$LFS = 20 \cdot \log_{10} \left(\frac{\lambda}{4 \pi d} \right) = 74 \, dB$$

 $P_{RX} = P_{TX} + G_{TX} - LFS + G_{RX} = 10+8-74+8=-48dBm$

$$LB = P_{RX} - S_{i} = -48 \text{ dBm} + 60 \text{ dBm} = 12 \text{ dB}$$



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Channel Capacity

Shannon's channel capacity, C [b/s]

 $C = \Delta f \cdot log_2(1 + SNR)$

- Fundamental limit for single TX-RX systems
- Improved with spatial diversity:multiple TX, RX)
 - Multiple-Input-Multiple-Output (MIMO)
 - all channels are statistically independent
 - require nonlinear data processing to improve SNR => expensive
 - Phased Arrays
 - at least part of TX, RX is shared
 - Linear: delay + sum processing

Phase Array

- Used in Marconi's 1901 transatlantic radio transmission
- First electronically steered phased arrays in WWII



True time delay

Phase delay

Variable phase vs. variable group delay

f

Phase



Group Delay



Properties of Phased Arrays (i)

• The signal before reaching the delay cell *i*

$$\mathbf{s}_{i}(t) = \mathbf{G}_{vi} \mathbf{A} \cos \left(\omega \left[t - (i - 1) \frac{\mathbf{d}}{\mathbf{c}} \sin(\theta_{in}) \right] \right)$$

To compensate for the propagation delays

$$\Delta \tau = \frac{d}{c} \sin(\theta_{in})$$

After summing node, signal scales linearly in N

$$\mathbf{s}_{\text{out}}(t) = \sum_{i=1}^{N} \mathbf{G}_{v} \mathbf{A} \cos[\omega[t - (i - 1)\frac{d}{c}\sin(\theta_{\text{in}}) + i\Delta\tau]] = \mathbf{N}\mathbf{G}_{v} \mathbf{A} \cos[\omega(t + \Delta\tau)]$$

Phased Array Parameters

 Array gain (factor) =power gain of array divided by power gain of single element

$$P_{in} = (N/2)A^2$$
, $P_{out} = N^2G^2A^2/2$, $G = P_{out}/P_{in} = NG^2_V$

 Beam-pointing angle = angle of incidence for which the array gain is maximized

$$\theta_{\rm m} = \arcsin\left(\frac{{\rm c}}{{\rm d}}\,\Delta\,\tau\right)$$

• **Beam width** = λ/L where L = (N-1)d

Typically d = $\lambda/2$

Benefits of Phased Arrays

- increased signal level at receiver output (the aggregate antenna gain increases N times)
- increased overall output power, scales with N
- Increased *EIRP* which scales as N^2
- immunity to interferers, but only within the bandwidth of each receiver and only after the signal-summation block,
- immunity to multi-path fading through antenna diversity in both RX and TX.

SNR and P_{out} Improvement



Ex. 60-GHz LOS, NLOS link budgets





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Automotive Radar

•An FMCW Doppler radar = a direct conversion radio



•Link Budget Equation

$$\mathsf{P}_{\mathsf{RX}} = \frac{\lambda^2 \sigma \mathsf{P}_{\mathsf{TX}} \mathsf{G}_{\mathsf{TX}} \mathsf{G}_{\mathsf{RX}}}{(4 \pi)^3 \mathsf{r}^4}$$

 σ is the radar cross section of the target in m².

FMCW Radar Waveforms





Radioastronomy and remote sensing

•W-band and D-Band "cameras" ("full body scanners")

Iow-noise, broadband receiver measuring "black-body"

radiation emitted by all bodies: $P = k\Delta fT$



Reference: Pozar

Total Power Radiometers

 T_A = antenna noise temperature T_R = receiver noise temperature T_s = system noise temperature R = detector responsivity [V/W] NEP = noise equivalent power

$$V_{o} = (kT_{B}\Delta f_{RF} + kT_{S}\Delta f_{RF})GR$$





Detector NEP



100Hz...10M Hz

Example of Total Radiometer

•94-GHz total power radiometer

• Δf_{RF} =10 GHz, G = 30dB (1000), T_S = 400K and τ = 20 mS,

 ΔT_{MIN} = 0.028 K.

This is an outstanding resolution!

If the LNA gain fluctuates by 0.05dB, ΔT_{MIN} increases dramatically to 4.62 K,

•For most practical applications, a resolution of at least 0.5 K is considered necessary.

Dicke Radiometer



Reduces impact of 1/f noise and gain fluctuations

Fiber and Backplane Systems

Fiber

Direct modulation ASK (OOK) transmitter

Direct detection receiver

New systems at 110+ Gb/s are based on QPSK and 16QAM

Backplane and cable transceivers

Unique example of a baseband system

No carrier modulation

NRZ or 4/8/128-PAM data transmission directly over backplane or cable


Amplitude Shift Keying

 $s(t)=m(t)cos(\omega_{o}t)$ where m(t)=0,1

- m(t) = data signal
- $\cos(\omega t) = carrier$
- Generation:
 - By upconversion: mixing data with carrier
 - By direct modulation: oscillator+ on-off switch
- Demodulation
 - Synchronously (coherent) by downconversion + lowpass filter (LPF)
 - Asynchronously (direct detection): square law or envelope detector +LPF

Amplitude Shift Keying (ii)

Coherent demodulation (better performance, costlier)

$$v(t) = s(t) \times \cos(\omega_0 t) = m(t) \cos^2(\omega_0 t)$$
$$\frac{1}{2} m(t) [1 + \cos(2\omega_0 t)] \rightarrow \frac{m(t)}{2}$$

$$P_{e} = \frac{1}{2} erfc \left(\sqrt{\frac{E_{b}}{4 n_{0}}} \right)$$
$$E_{b} = \int_{0}^{T} s^{2}(t) dt$$

$$b \quad \mathbf{J} \quad \mathbf{t} = 0$$

$$P_{e} = \frac{1}{2} erfc \left(\sqrt{\frac{SNR}{4} \frac{\Delta f}{R_{b}}} \right)$$

- P_e = probability of error in detector E_b = energy of signal over 1 bit period in Ws n_0 = noise power spectral density in W/Hz R_b = data rate
- $\Delta f =$ bandwidth

Amplitude Shift Keying (iii)

Direct detection (1dB worse SNR)

$$v(t) = s^{2}(t) = m^{2}(t) \cos^{2}(\omega_{0}t)$$
$$\frac{m^{2}(t)}{2} [1 + \cos(2\omega_{0}t)] \rightarrow \frac{m^{2}(t)}{2} = \frac{m(t)}{2}$$

Frequency Shift Keying

Carrier frequency switches between two values f₁, and f₂, generated with VCO, constant amplitude, no need for linear power amplifier

 $s(t) = cos[(\omega_2 + m(t)\Delta\omega)t]$

Where

- m(t) is a binary data signal,
- $\Delta \omega = 2\pi \Delta f$ and
- $\Delta f = f_1 f_2$.
- Spectrum effective bandwidth

T= period of binary data signal

$$B=2\left(\Delta f+\frac{2}{T}\right)$$

Frequency Shift Keying: Detector





Phase Shift Keying

 $s(t) = m(t) cos(\omega_o t)$

Where m(t) is in polar NRZ format, i.e. m(t) = +/-1

- Generation:
 - mixing(upconversion) m(t) with carrier $cos(\omega_0 t)$
 - Direct phase (sign) modulation of differential VCO signal
- As FSK, has constant amplitude, good with non-linear power amplifiers

Phase Shift Keying: Detection

Only coherently (as coherent ASK)

$$v(t) = s(t) \times \cos(\omega_0 t) = m(t)\cos^2(\omega_0 t)$$
$$\frac{1}{2}m(t)[1 + \cos(2\omega_0 t)] \rightarrow \frac{m(t)}{2}$$

 Difference from ASK: m(t) is polar, hence decision threshold =0, does not depend on amplitude

$$P_{e} = \frac{1}{2} erfc \left(\sqrt{\frac{E_{b}}{n_{o}}} \right)$$

 P_e is 6 dB better than ASK and 3 dB better than FSK, but ASK has 3 dB lower average transmit power