Isaac Physics Skills

Developing mastery of

Essential pre-university physics

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Essential pre-university physics
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Developing problem solving skills

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These sheets are of two kinds - skill sheets and fact sheets and are equally valuable in both the early stages of learning and in revision.

The skill sheets provide practice for the student in applying a single principle of physics to a range of reasonably straightforward situations - often starting out with the substitution of values into an equation. After the first few questions have enabled the student to gain confidence in using the equation, subsequent questions may require the use of more than one equation or principle, or insight to solve a novel problem.

The fact sheets test knowledge on the parts of sixth form physics courses which require reading. While eminently suitable for revision, they may also be used to verify that the student has performed prior reading on the operation of an MRI scanner, for example, before it is discussed in class.

While the manner of use is up to the teacher and the student, we recommend that until a pass mark (we suggest 75%, as indicated in the square by each skill sheet) is obtained, the student studies further, then repeats a selection of questions. This process is repeated until the student passes. This is our understanding of applying a mastery method to ensure a good foundation is laid for a pre-university physics education. The teacher's mark book records how many attempts the student has taken rather than the mark obtained on a sole attempt. Students, likewise, have a list of the skills, and tick them off when the required level of proficiency has been obtained. A grid is provided at the front of this book for this very purpose. In this way, all students achieve mastery of the skills, and do not move on until this has been achieved. We have found that all students who have the capacity to pass an A-level course have the capacity to attain mastery of all of these skills. However, we find that if such mastery has been obtained, the student goes on to gain a greater understanding of physics and a higher grade at A-level than would be expected otherwise.

We also recommend that an answer is not considered correct unless it is numerically accurate, is given to an appropriate number of significant figures, and incorporates a suitable unit: a student cannot be satisfied with their comprehension while they are still getting the final result incorrect. After all, this would be intolerable in any practical situation in which physics principles were applied. The Isaac Physics on-line version of this book, and its associated marking facility, follow these significant figure and unit requirements.

A mapping of each set of exercises in the book onto the 6 major school exam specifications in the UK is given on-line at isaacphysics.org/pages/syllabus_map where, with a click, the appropriate part of the book can be accessed and the problems solved or set as homework.

 $^{n}/_{m}$

Acknowledgements

These sheets, and the approach presented here for using them, were first devised for use in the Physics Department at the Royal Grammar School in High Wycombe, where we served as colleagues from 2010 to 2014. We are grateful to the students who have put them to such productive use, and have given valuable feedback. We are also grateful to colleagues in other schools who have also applied these methods and given us encouragement – particularly Keith Dalby at Westcliff High School for Boys.

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And finally, we thank you for being willing to try them out too. We wish you well with your studies, and hope that these sheets help you and your students attain understanding and success.

Soli Deo Gloria,

ACM & JJC Westcliff-on-Sea & High Wycombe, 2015

Using Isaac Physics with this book

Isaac Physics offers on-line versions of each sheet at isaacphysics.org/books/physics_skills_19 where a student can enter answers. This on-line tool will mark answers, giving immediate feedback to a student who, if registered on isaacphysics.org, can have their progress stored and even retrieved for their CV! Teachers can set a sheet for class homework as the appropriate theme is being taught, and again for pre-exam revision. Isaac Physics can return the fully assembled and analysed marks to the teacher, if registered for this free service. Isaac Physics zealously follows the significant figures (sf) rules below and warns if your answer has a sf problem.

Uncertainty and Significant Figures

In physics, numbers represent values that have uncertainty and this is indicated by the number of significant figures in an answer.

Significant figures

When there is a decimal point (dp), all digits are significant, except leading (leftmost) zeros: 2.00 (3 sf); 0.020 (2 sf); 200.1 (4 sf); 200.010 (6sf)

Numbers without a dp can have an absolute accuracy: 4 people; 3 electrons.

Some numbers can be ambiguous: 200 could be 1, 2 or 3 sf (see below). Assume such numbers have the same number of s.f. as other numbers in the question.

Combining quantities

Multiplying or dividing numbers gives a result with a number of sf equal to that of the number with the smallest number of sf:

x = 2.31, y = 4.921 gives xy = 11.4 (3 sf, the same as x).

An absolutely accurate number multiplied in does not influence the above.

Standard form

On-line, and sometimes in texts, one uses a letter 'x' in place of a times sign and $\hat{}$ denotes "to the power of":

1800000 could be 1.80x10⁶ (3 sf) and 0.0000155 is 1.55x10⁻⁵

(standardly, 1.80×10^6 and 1.55×10^{-5})

The letter 'e' can denote "times 10 to the power of": 1.80e6 and 1.55e-5.

Significant figures in standard form

Standard form eliminates ambiguity: In $n.nnn \times 10^n$, the numbers before and after the decimal point are significant:

 $191 = 1.91 \times 10^2$ (3 sf); 191 is $190 = 1.9 \times 10^2$ (2 sf); 191 is $200 = 2 \times 10^2$ (1 sf).

Answers to questions

In this book and on-line, give the appropriate number of sf: For example, when the least accurate data in a question is given to 3 significant figures, then the answer should be given to three significant figures; see above. Too many sf are meaningless; giving too few discards information. Exam boards also require consistency in sf.

Physical Quantities

Quantity	Magnitude	Unit
Permittivity of free space (ϵ_0)	8.85×10^{-12}	F m ⁻¹
Electrostatic force constant $(1/4\pi\epsilon_0)$	8.99×10^9	N m ² C ⁻²
Speed of light (in vacuo)	3.00×10^{8}	$\mathrm{m}\mathrm{s}^{-1}$
Universal gravitational constant (G)	6.67×10^{-11}	N m ² kg ⁻²
Avogadro constant ($N_{\rm A}$)	6.02×10^{23}	mol ⁻¹
Boltzmann constant (k _B)	1.38×10^{-23}	J K ^{−1}
Gas constant (R)	8.31	J mol ⁻¹ K ⁻¹
Planck constant (h)	6.63×10^{-34}	Js
Charge of proton (e)	1.60×10^{-19}	С
Electron volt (eV)	1.60×10^{-19}	J
Unified atomic mass unit (u)	1.66054×10^{-27}	kg
Mass of neutron (m_n)	1.67493×10^{-27}	kg
Mass of neutron (m_n)	1.00867	u
Mass of proton (m _p)	1.67262×10^{-27}	kg
Mass of proton (m _p)	1.00728	u
Mass of electron (m_e)	9.10938×10^{-31}	kg
Mass of electron (m_e)	5.48580×10^{-4}	u
0 °C	273.15	K
1 parsec (pc)	3.086×10^{16}	m
Acceleration due to gravity (g)	9.81	$\mathrm{m}\mathrm{s}^{-2}$
Seconds per year	3.156×10^{7}	-
Light year	9.46×10^{15}	m
Specific heat capacity of water	4180	J kg ⁻¹ K ⁻¹

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Checklists

Unit	Skill	
A1	Choose an appropriate equation from a list, re-arrange it, substitute	
	numbers for variables, and calculate the unknown quantity.	
A2	Express units in terms of SI base units.	
A3	Express a measurement in standard form (2.43×10^{-8}) or using a	
	prefix (24.3 ns) to a given number of significant figures.	
A4	Convert measurements from one unit to another.	
A5	Calculate the gradient or y-intercept of a straight line on a graph and give its unit.	
A7	Estimate the area under the line on a graph and give its unit.	
A8	Estimate areas under lines using units with prefixes.	
A9	Calculate changes in response to changes by factors & percentages.	
A10	Calculate changes when a proportionality is known.	
B1	Determine the horizontal and vertical components of a vector (dis-	
	placement, velocity, force or the electric field in Malus' Law).	
B2	Determine the sum of two vectors by scale drawing or trigono-	
	metry where the triangle of vectors always has a 90° angle.	
В3	Solve problems of uniform accelerated motion in 1-dimension	
	(SUVAT problems).	
B4	Solve trajectory problems using the independence of horizontal	
	and vertical motion.	
B5	Find the missing force in a question using the principle of moments.	
В6	Stress, strain and Young's modulus.	
B7	Force & energy calculations for springs separately & combined.	
B8	Mechanical calculations of energy and power.	
В9	Energy and force in springs and stretched materials.	
C1	Resistors & resistivity.	
C2	Understands the relationship between charge carrier motion and	
	electric current.	
C4	Solve circuit problems using Kirchhoff's Laws.	
C5	Find the voltage across components in a potential divider circuit.	
C6	Work out the terminal p.d. of a battery given the current supplied,	
	e.m.f. and internal resistance.	
D1	Calculate amplitudes and intensities from power.	
D2	Intensities of light after passing a polarizer.	
D3	Determine whether a wave, traveling by two different routes to a	
	detector will interfere constructively or destructively.	

Unit	Skill	\neg
D4	Select the right equation to use for two-source interference prob-	
	lems, re-arrange it, and solve it to obtain the correct answer.	
D5	Understand standing waves.	
D6	Select an equation to use in solving photoelectric effect problems,	
	re-arrange it, and solve it to obtain the correct answer.	
D7	Perform calculations relevant to quantum physics.	
D8	Calculate refractive indices, angles of refraction, and critical angles.	
D9	Calculate electromagnetic spectra from atomic energy schemes.	
E1	Estimate absolute uncertainties.	
E2	Calculate relative uncertainties.	
E3	Estimate the relative uncertainty in a calculated result from the	
	uncertainties of the original measurements.	
E4	Assess whether measurements are accurate or reliable.	
F1	Calculate the force needed to change an object's momentum in a	
	given time.	
F2	Solve a 1-d problem in conservation of momentum.	
F3	Convert angles from degrees to radians, can convert ordinary	
	speeds into angular speeds, can convert between frequency, time	
	period & angular frequency.	
F4	Work out the size and direction of the force needed to keep an	
775	object in uniform circular motion.	
F5	Work out the gravitational force on an object using Newton's law of	
	gravity, either directly (knowing <i>M</i>) or by comparison with another	
E(object where the force is known.	
F6	Work out the time period of a circular orbit from its radius (or vice	
F7	versa) without looking up Kepler's 3rd Law. Perform calculations related to oscillators.	_
G1	Convert Celsius into kelvin, and know when K must be used.	_
G1 G2	Use the right form of the gas law $(pV=nRT \text{ or } pV = NkT \text{ or } pV = $	
G2	pV/ T =const) to solve a problem involving gases.	
G3	Calculate energies required to cause temperature changes, and to	
GS	calculate the final temperature of mixtures.	
G4	Calculate the infairtemperature of infatures. Calculate energies required to cause changes of state.	_
H1	Work out the force (direction & magnitude) on an electron or alpha	\dashv
111	particle between two charged plates.	
H2	Calculate the electric field <i>E</i> near one or two point charges.	\dashv
H3	Find the speed of electrons accelerated from rest in an electric field.	\dashv
110	That the opeca of electrons accelerated from rest in an electric field.	

x CHECKLISTS

Unit	Skill			
H4	Work out the force (direction & magnitude) on a wire carrying a			
	current in a magnetic field.			
H5	Work out the force (direction & magnitude) on a moving charged			
	particle in a magnetic field.			
H6	Work out the radius of the circular path followed by a charged			
	particle in a magnetic field.			
H7	Work out the e.m.f. (magnitude & direction) induced in a coil of			
	wire when it is moved in a magnetic field.			
H8	Calculate the voltage on the secondary of a transformer.			
H9	Calculate energies and potentials of charges in electric fields.			
I1	Work out the charge & energy stored on a capacitor from the char-			
	ging voltage.			
I2	Work out the capacitance of a network of capacitors.			
I3	Sketch the current / voltage / charge on a capacitor as a function of			
	time as it discharges through a resistor, labelling key points.			
J1	Complete a nuclear equation (including beta decay and neutrinos.)			
J2	Calculate the half life of a radioactive sample from a knowledge of			
	number of nuclei & activity.			
J3	Sketch the no. of nuclei remaining in / activity of a radioactive			
	source as a function of time as it decays, labelling key points.			
J4	Calculate the energy released in a nuclear reaction from the masses			
	of reactants & products OR a graph of binding energy per nucleon.			
K1	Work out galaxy velocity from spectral shift and thus its distance			
	using Hubble's law.			
K2	Perform a variety of exponential calculations.			

Explanation Checklist

Unit	Skill	
L1	How a mass spectrometer works.	
L2	The main categories of fundamental particles.	
L3	The construction of a nuclear (fission) reactor.	
L4	What happens when X-rays hit tissue, and how X-ray images can	
	be improved.	
L5	How an ultrasound image is taken, the significance of acoustic	
	impedance, and the difference between A and B scans.	
L6	How MRI works, and the advantages & disadvantages of MRI in	
	comparison with other techniques (X-ray, PET).	
L7	The life cycle of a star.	
L8	The history of the Universe according to the Big Bang model.	

Chapter A

General Questions

The boxed fraction shows how many questions need to be answered correctly to achieve mastery.

A1 Using and Rearranging Equations

⁹/₁₂

Use the following equations:

$$s = ut$$
 $a = \frac{(v - u)}{t}$ $F = ma$ $v = f\lambda$
 $V = IR$ $P = IV$ $E = Pt$ $Q = It$

where the letters have the following meanings:

$$s = \text{distance}$$
 $u, v = \text{velocity}$ $t = \text{time}$ $m = \text{mass}$ $V = \text{voltage}$ $I = \text{current}$ $F = \text{force}$ $a = \text{acceleration}$ $Q = \text{charge}$ $E = \text{energy}$ $P = \text{power}$ $f = \text{frequency}$ $A = \text{wavelength}$ $R = \text{resistance}$

- A1.1 a) F = 3.0 N, m = 2.0 kg, what is a?
 - b) I = 0.20 A, t = 200 s, what is Q?
- A1.2 Calculate the resistance needed if you want 0.030 A to flow through a component when a 9.0 V battery is connected to it.
- A1.3 Calculate the distance travelled by a car going at $30 \,\mathrm{m\,s^{-1}}$ in 2.0 minutes.
- A1.4 Calculate the wavelength of a wave that travels at 3.0×10^8 m s⁻¹ if its frequency is 2.0 GHz (2.0×10^9 Hz).
- A1.5 a) Calculate the power of a 0.25 A, 240 V light bulb.

- b) Calculate the power if 5.0 A flows through a 2.0 Ω resistor.
- A1.6 A Corsa accelerates from 15 m $\rm s^{-1}$ to 25 m $\rm s^{-1}$ in 8.0 s. Calculate the acceleration.
- A1.7 If a jet has a maximum acceleration of 20 m s⁻², what is the time it would take to get from 0 m s^{-1} to 100 m s^{-1} ?

 A1.8 My kettle needs to be able to give $672\,000 \text{ J}$ of heat energy to water in
- A1.8 My kettle needs to be able to give 672 000 J of heat energy to water in 240 s. Assuming that it is connected to the 240 V mains, what current is needed?
- A1.9 Calculate the force needed if my 750 kg car needs to accelerate from rest to 13 m s^{-1} in 5.0 s.
- A1.10 Calculate the electrical energy used by a 240 V light bulb with a resistance of 60 Ω in 600 s.



A2 Derived and Base SI Units

Express the following derived units in terms of the SI base units. The first one has been done for you:

	Derived Unit	in Base Units	Power of each base un		oase unit	
			m	S	kg	A
	$\mathrm{m}~\mathrm{s}^{-2}$	$\mathrm{m}~\mathrm{s}^{-2}$	1	-2	0	0
A2.1	J		(a)	(b)	(c)	(d)
A2.2	N		(a)	(b)	(c)	(d)
A2.3	С		(a)	(b)	(c)	(d)
A2.4	V		(a)	(b)	(c)	(d)
A2.5	Ω		(a)	(b)	(c)	(d)
A2.6	Pa		(a)	(b)	(c)	(d)
A2.7	N C ⁻¹		(a)	(b)	(c)	(d)
A2.8	$V m^{-1}$		(a)	(b)	(c)	(d)

Express the following derived units in terms of the unit specified and base units. The first one has been done for you.

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		1					
A2.9	a) Express the ohm in terms of	the volt and base units: $\Omega = V A^{-1}$					
	b) Express the joule in terms of	the newton and base unit(s).					
	c) Express the pascal in terms of	Express the pascal in terms of the joule and base unit(s).					
	d) The answer to (c) means the amount of energy per unit	nat pressure in effect measures an					
	e) Express the $V m^{-1}$ in terms o	f the joule and base unit(s).					
	f) Express the unit of density in	n newtons and base unit(s).					
A 3	Standard Form and Prefixe	s					
wher	re the question specifies the requi	wrong number of significant figures ired number of significant figures. e is always one non-zero digit before					
A3.1	Write the following as 'normal' nu	ımbers:					
	a) 3×10^4	b) 4.89 × 10 ⁶					
A3.2	Write the following as 'normal' nu	umbers:					
	a) 3.21×10^{-3}	b) 2×10^0					
A3.3	Write the following in standard for a) 2 000 000	orm to three significant figures: b) 34580					
A3.4	Write the following in standard for a) 23.914	orm to three significant figures: b) 0.000 005 638					
A3.5	the prefix):	numbers with the unit (but without					
	a) 3 kJ	b) 20 mA					
A3.6	Write the following using the mos a) 5×10^7 m	st appropriate prefixes: b) 6×10^{-10} s					

9/11

A4 Converting Units

Convert between units as specified. Express your answer in standard form if the power of ten is ≥ 3 , or ≤ -3 . Your answer must include units, as indeed it must in *all* questions with units in this book.

Convert:

A4.1 a) 34.5 mm to nm

b) 34.5 mm to pm

A4.2 2.4 ps to ms

A4.3 a) $465 \mu A$ to mA

b) 465 μA to kA

A4.4 43×10^{-7} GW to μW

A4.5 $34 \text{ m}^2 \text{ to cm}^2$

A4.6 58 N m to N cm

A4.7 9600 μm^2 to cm²

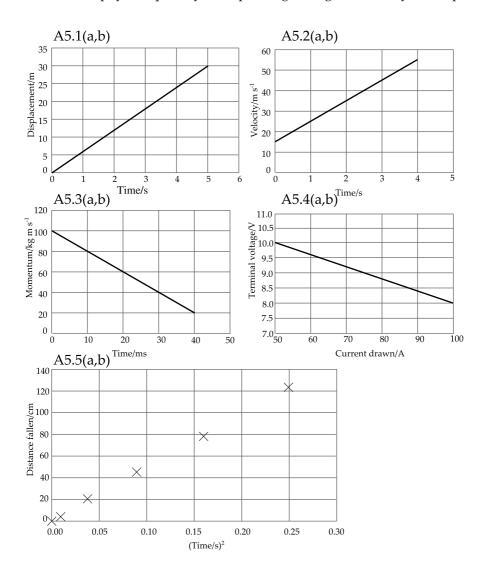
A4.8 0.035 N cm^{-2} to Pa

 $A4.9 ext{ } 450 ext{ kg m}^{-3} ext{ to kg mm}^{-3}$

A5 Gradients and Intercepts of Graphs

⁸/₁₀

Work out the physical quantity corresponding to the gradient and y-intercept.



Chapter F

Mechanics

 $^{8}/_{10}$

F1 Force and Momentum

In these questions ignore the effects of friction & drag.

- F1.1 What is the momentum of a 750 kg car going at 31 m s $^{-1}$?
- F1.2 What is the momentum of an electron (mass = 9.1×10^{-31} kg) travelling at 3.0×10^7 m s⁻¹?
- F1.3 If a 20 000 kg bus accelerates from 10 m s^{-1} to 25 m s^{-1} , what is the change in momentum?
- F1.4 A 50 g ball is travelling at 2.0 m $\rm s^{-1}$ when it hits a wall and rebounds at 1.5 m $\rm s^{-1}$. Calculate the change in momentum.
- F1.5 A 750 kg car takes 15.3 s to accelerate from 5.0 m s⁻¹ to 31 m s⁻¹. Calculate the force needed to do this.
- F1.6 A 70 kg person jumps in the air and is travelling downwards at 2.0 m s⁻¹ when their feet touch the ground. If it takes the person 0.30 s to stop, calculate the resultant force on them.
- F1.7 I am trying to push start a car which has stopped. If the biggest force with which I can push the car is 420 N, and the car has a mass of 1025 kg, how fast will it be going after 8.0 s of pushing?
- F1.8 Calculate the force needed to accelerate a $50\,000$ kg spacecraft from rest to 7000 m s⁻¹ in four minutes.
- F1.9 An alpha particle (mass = 6.7×10^{-27} kg) is fired at the nucleus in a gold atom with a speed of 3.5×10^6 m s⁻¹. It bounces off at the same speed in the opposite direction. If the collision takes 10^{-19} s, what is the average force?
- F1.10 How long would it take a 637 N force to accelerate a 65 kg physics teacher from rest up to a speed of 100 m s⁻¹? (NB this is over 200 mph)

F2 Conservation of Momentum

F2.1 Two masses, called Alfie and Beth, collide and stick together under four different circumstances, as shown in the four rows of the table below. Calculate the missing measurements:

	After collision			
Alfie's mass/kg	Alfie's velocity /m s ⁻¹	Beth's mass /kg	Beth's velocity /m s ⁻¹	Velocity /m s ⁻¹
30	+2.0	40	+1.5	(a)
60	-1.4	30	+2.8	(b)
120	+1.5	80	(c)	0.0
120	+3.0	(d)	-31	+2.0

- F2.2 Charlie is driving her $20\,000$ kg bus. She stops at a roundabout. Percy is driving his 750 kg Corsa at 15 m s⁻¹ behind her. He fails to stop and rams into the back of the bus, sticking to it. The impact releases the brakes on the bus. How fast will the smashed up wreck be travelling immediately after the collision?
- F2.3 A neutron (mass = 1 u) is moving at 300 m s⁻¹ when it smacks into a stationary 235 U nucleus (mass = 235 u), and sticks to it. What will the velocity of the combined particle be?
- F2.4 A 7.90 g bullet is travelling at 200 m s $^{-1}$. It hits a 3.00 kg sack of sand which is hanging by a rope from the ceiling. The bullet goes into the sack, and is stopped inside it by friction with the sand. How fast is the sack going immediately after the bullet has "stopped" inside it 1 ? NB you must give your answer to 3 significant figures to be awarded the mark.
- F2.5 A rocket (containing a space probe) is travelling at 7000 m s $^{-1}$ in outer space. The 2000 kg probe is ejected from the front of the rocket (forwards) using a big spring. If the speed of the probe afterwards is 7200 m s $^{-1}$, and the rest of the rocket has a mass of 6000 kg, what is the speed of the rest of the rocket?

 $^{8}\!/_{10}$

¹"stopped" means stopped relative to the sand, not stopped relative to a stationary observer.

- F2.6 In a strange form of billiards, the cue ball is one third the mass of the other balls, which are stripey. There is no spin, and I hit a stripey ball centrally with the cue ball (travelling at 1.4 m s⁻¹) such that the cue ball rebounds in the opposite direction with half of its initial speed. What is the speed of the stripey ball?
- F2.7 I am stranded, stationary, in space, but near to my spacecraft. I detach my 30 kg oxygen cylinder, and fling it away from the spacecraft with a speed of 3.0 m s^{-1} . If my mass (without the cylinder) is 80 kg, how fast will I travel in the other direction towards my spacecraft?

 $^{18}\!/_{20}$

F3 Units of Rotary Motion

- F3.1 How big is 3 rad, when expressed in degrees?
- F3.2 How many radians are there in 90°?

Complete the questions in the table by converting the units:

	Time period /s	Fre- quency /Hz	Angular Velocity /rad s ⁻¹	Revolutions per Minute (rpm)
F3.3	0.50	(a)	(b)	(c)
F3.4	(a)	(b)	3.0	(c)
F3.5	(a)	(b)	(c)	3800
F3.6	(a)	50	(b)	(c)
F3.7	2700	(a)	(b)	(c)

- F3.8 A car travels 10 km. One of its wheels has a radius of 30 cm. Calculate the angle the wheel turns as the car travels this distance (answer in radians).
- F3.9 An astronaut's training centrifuge has a radius of 4.0 m. If it goes round once every 2.5 s, calculate the velocity of the end of the centrifuge arm (4.0 m from the pivot).
- F3.10 My washing machine has a spin speed of 1200 rpm, and a drum radius of 20 cm. Calculate how fast clothes go, when up against the side of the drum.

Isaac Physics

Developing problem solving skills.

L. Jardine-Wright

Director, Isaac Physics Project

About the author

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LJW, 2020

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Developing Physics Problem Solving

Isaac Physics - You work it out

isaacphysics.org

The key concepts and numerical manipulations that you practise in Chapters A - L are the vital step on the road to studying physics, engineering or any STEM course at university. To further advance your thinking as a physicist, you also need to enhance these skills and this analysis by combining multiple concepts and techniques, in order to solve longer and more involved problems. These multi-step, multi-stranded questions can be challenging for experienced physicists, but completion of such problems gives a real sense of achievement and success.

The main mission of Isaac Physics is to provide problem solving questions for students at GCSE (or equivalent) through to those who have finished their A-levels and are preparing for university. We have over 850 questions graded from Level 1 (post-GCSE) through to Level 6 (pre-university and beyond – NOT for the fainthearted).

In the following chapters you will find:

- · advice on how to problem-solve,
- sample solutions to two problems from our site (Level 3 Dynamics: Pop-up Toy, and Level 5 Statics: Prism)
- sample questions from mechanics and fields, from our six levels on isaacphysics.org
 Online, we also have the topics: waves, circuits and physical chemistry.
 They too span all six levels, with questions for you to try.
- next to each topic heading, a url link to a webpage containing this and the other questions from the same level and topic.

Take up the challenge and put your new found skills to the test — but before you do, make sure you pick up a large **pad of paper** and **a pencil** so that **you** can work it out.

A Guide to Solving Physics Problems

isaacphysics.org/solving_problems

Physicists develop highly desirable skills through their extensive experience of problem solving — logic, determination, resilience and mathematical ability to name just a few. You will become an ace problem solver by answering *lots* of questions — these 5 key steps will help you develop a logical, structured method and universal approach.

5 key steps to problem solving

- · Step 1: Keywords
- · Step 2: Diagram
- · Step 3: Concepts
- Step 4: Symbols
- · Step 5: Dimensions & Numbers

When faced with a new question, we employ a strategy to break the problem down into a series of 5 steps to digest and analyse it. Each step helps us to understand the information given in the question and establish what it is that we are being asked to calculate or discover. Using these steps for each new question we attempt can, with practice, make solving physics problems extremely satisfying and rewarding.

Step 1: Keywords

Are there words in the question that contain additional information about the problem? Frictionless; light; uniform... Highlight these words so that they stand out — they will help to simplify the solution and allow us to neglect concepts that we don't need to consider.

Step 2: Draw a diagram

The action of drawing a diagram helps us to digest and summarise the information in a question. Drawing a diagram will save time and effort later and is the key to finding a solution. When drawing the diagram, label the quantities that are given with symbols (e.g. u for a velocity, d for a displacement); staying in symbols rather than using numbers is vital — see Step 4.

Step 3: Key concepts & mathematics

Fluency with mathematical rearrangements is essential but we need to

be sure that we are logical with our approach and consider the physical concepts that we need before throwing algebra at the problem. Identify which concepts are relevant to the problem. Write down the relevant physical principles and equations that might be useful — particularly if they connect the quantities that are given in the question.

Step 4: Stay in symbols

Even if the question gives numerical values, represent each of them with a symbol. This may appear to overcomplicate the problem, but it really helps when checking the solution or trying to find a mistake.

For example, imagine that as part of the calculation we want to find the magnitude of the displacement, $|\underline{d}|$, of a cyclist who has travelled 13 km West and 5.0 km North.

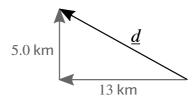


Figure 1: The displacement of a cyclist who has travelled 13 km West and 5.0 km North.

You identify that you need to use Pythagoras' theorem

$$|\underline{d}| = \sqrt{144} = 12 \,\text{km} \qquad \text{WRONG} \qquad (1)$$

The numbers hide information about the calculation that letters would not. Let $w=13\,{\rm km}$ and $n=5\,{\rm km}$

$$|\underline{d}| = \sqrt{w^2 - n^2} = 12 \,\mathrm{km}$$
 WRONG (2)

You can see straight away that the square of the numbers have accidentally been subtracted rather than added.

• Step 5: Check dimensions, then put in numbers, check if reasonable Before putting numbers into an algebraic expression, experienced physicists check whether their answer has the correct *dimensions* (you may have seen this before as checking your units). For example, if we are trying to find a quantity of time, *each term* in our expression must have dimensions of *only* time — no length, or mass or charge!

Imagine that we are trying to calculate how fast the Earth travels around the Sun and we know that the radius of the Earth's orbit is $r=1.50\times10^{11}\,$ m and that it takes $t=365.25\,$ days. We make a mistake and write down that

the distance travelled by the Earth is $2\pi r^2$. If we check our dimensions on both sides of the equation, we can see that this is incorrect.

speed =
$$\frac{2\pi r^2}{t}$$
 (3)

speed
$$=$$
 $\frac{2\pi r^2}{t}$ (3)
Dimensions: $\frac{[L]}{[T]} \neq \frac{[L]^2}{[T]}$

The length dimension, [L], that we have on the top of the left hand side of expression (4) does not match the length squared, $[L]^2$ on the top of the right hand side of expression, so we determine that there is a mistake with our r^2 part of the expression.

Lastly, we put in the numbers and, vitally, check the magnitude of our answers – are they reasonable?

Now we have the steps, we apply them to two example problems from Levels 3 and 5 of isaacphysics.org.

Example Solution - Level 3 Dynamics: Pop-up Toy

isaacphysics.org/s/i80Q9P

Q: A pop-up toy consists of a head and sucker of combined mass m = 1.5 kgstuck to the top of a light spring of natural length $l_0 = 0.30$ m and spring constant $k = 250 \text{ N m}^{-1}$. The centre of mass of the system can be taken to be at the top of the spring. The spring is compressed to length $l_1=0.10\,\mathrm{m}$ when the pop-up toy is stuck to the ground.

What height above the ground does the bottom of the unstretched spring jump to when it is smoothly released?

Step 1: Keywords

Highlight the key words in the text above.

What are the key words in the question that will help you to draw your diagram and understand the physical concepts that might be useful? Note also what the question is asking for.

Solution:

- combined mass at the top we can consider the sucker and mass as one object of mass m at the top of the spring.
- centre of mass the point at which we should consider the weight of the combined mass to act.

- light we can consider the spring to have no mass or weight, it is negligible.
- spring is extensible.
- smoothly released the toy is not caused to jolt in anyway so there is no energy converted to heat or sound; we conserve kinetic and potential energies.
- Q: Height of the bottom of the spring.

Step 2: Draw a diagram

Draw and annotate a diagram with all of the information from the question, in particular draw each stage of the toy's behaviour.

Solution:

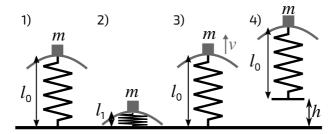


Figure 2: The 4 stages of the toy's behaviour. 1) Before compression. 2) Compressed and ready to jump. 3) Returned to its natural length, l_0 , but now the mass and sucker has a velocity, v. 4) At maximum height, the velocity of the mass and sucker = 0.

Steps 3 & 4: Concepts, mathematics & symbols

Identify the concepts that you think might be useful in answering the question. Doing this gets you started. Some ideas might not get used.

Solution: Hooke's Law, spring constant, forces, work done, gravitational potential energy (GPE), elastic potential energy (EPE), kinetic energy (KE) and conservation of energy.

Method 1: Energy

How do you know whether to analyse a problem using forces (method 2) or energy? Using conservation of energy in this problem is simpler, as the total amount of energy remains the same throughout all the stages of motion and therefore we can consider just the beginning and end situations (stage 2 and stage 4).

Write down an expression for the conservation of energy. The total energy of the toy at stage 2 is equal to its total energy at stage 4.

• Take care to define a position of zero gravitational potential energy.

Solution: For the whole of this solution I will choose for the ground level to be the position of zero gravitational potential energy.

Total energy at stage 2 = Total energy at stage 4

$$\begin{aligned} \mathsf{GPE}_2 + \mathsf{EPE}_2 &= \mathsf{GPE}_4 \\ mgl_1 + \frac{1}{2}k(l_0 - l_1)^2 &= mg(h + l_0) \\ h + l_0 &= l_1 + \frac{1}{2mg}k(l_0 - l_1)^2 \\ h &= l_1 - l_0 + \frac{1}{2mg}k(l_0 - l_1)^2 \end{aligned} \tag{5}$$

Method 2: Force and Work Done

Using a force method for the pop-up toy is more challenging because the force due to the spring is not constant throughout the motion. However, analysing the problem through forces should give us the same answer.

How does the force exerted by the spring on the mass cause the toy leap off the ground?

Solution: Hooke's Law tells us that the magnitude of the force, F, needed to compress a spring by an amount x, is given by F=kx. To compress the spring by an additional small amount δx we need to do work **on** the spring. The amount of work done is $\delta W=F\delta x$. As δx becomes very small (tends to zero), δW tends to dW.

We can then find the total work done to compress the spring from stage 1 to stage 2 by integrating with respect to dx between the limits of the compression at stage 1 to the compression at stage 2.

Stage 1, compression =
$$0$$

Stage 2, compression = $(l_1 - l_0)$.

The total work done on the spring between these two stages is then released between stages 2 and 4, and converted to gravitational potential energy.

Work done from 1 to 2 = change in GPE from 2 to 4

$$\int_{0}^{(l_{1}-l_{0})} (kx) dx = GPE_{2} - GPE_{4}$$

$$\left[\frac{1}{2}kx^{2}\right]_{0}^{(l_{1}-l_{0})} = mgl_{1} - mg(h+l_{0})$$

$$h + l_0 = l_1 + \frac{1}{2mg}k(l_1 - l_0)^2$$
$$h = l_1 - l_0 + \frac{1}{2mg}k(l_1 - l_0)^2$$

Our result is indeed consistent with that of method 1, equation (5).

This is not the only force method we could use, the problem can also be solved using Newton's Second Law to equate the resultant force on the toy, at a general time, to its acceleration. The acceleration must be written in terms of $\frac{\mathrm{d}v}{\mathrm{d}x}$ rather than $\frac{\mathrm{d}v}{\mathrm{d}t}$ so that we can then integrate to find an expression for v^2 which can be related to the height h.

Step 5: Dimensions & numbers

The question asks for a height, which has dimensions of length [L] — each term on the right of our expression (5) should therefore also have dimensions of length.

Solution: Not all of the terms have dimensions that we can just write down; for example, what are the dimensions of k and g?

$$g = \operatorname{acceleration} = [L][T]^{-2}$$

$$k = \frac{\operatorname{force}}{\operatorname{length}} = \frac{[M][L][T]^{-2}}{[L]} = [M][T]^{-2}$$

$$h = l_1 - l_0 + \frac{1}{2mg}k(l_0 - l_1)^2$$

$$= [L] + [L] + \frac{[1]}{[M][L][T]^{-2}}[M][T]^{-2}([L])^2$$

$$= [L] + [L] + [L] = \operatorname{correct}$$

Now we substitute the values given in the question and consider carefully the number of significant figures we should give in our answer.

$$m=1.5\,{
m kg}, l_0=0.30\,{
m m}, l_1=0.10\,{
m m}, k=250\,{
m N\,m^{-1}}$$
 and $g=9.81\,{
m m\,s^{-2}}.$

Solution:

$$h = l_1 - l_0 + \frac{1}{2mg}k(l_0 - l_1)^2$$

$$h = 0.10 - 0.30 + \frac{1}{2 \times 1.5 \times 9.81} \times 250 \times (0.30 - 0.10)^2 = 0.14 \,\mathrm{m}$$

Is this answer reasonable? 14cm is indeed a realistic height for the bottom of the spring to reach.

Example Solution - Level 5 Statics: Prism

isaacphysics.org/s/i80Q9P

A prism has a cross section that is an isosceles triangle. It has a unique angle of 30° , and a mass of $m=100\,$ g. You wish to lift it by touching the upper two faces only.

Q: If the coefficient of friction between the prism's surface and your skin is $\mu=0.400$, what is the minimum normal force you need to apply to each face in order to support the prism?

Step 1: Keywords

Highlight the key words in the text above.

What are the key words in the question? Note exactly what the question asks.

Solution: isosceles, friction, minimum, normal, unique angle.

Q: We are asked for the minimum normal force applied to **each** face.

Step 2: Draw a diagram

Redraw and annotate a diagram of the prism.

- Label your angle θ to stay in symbols until the end of the calculation.
- Annotate the diagram with all the forces acting on the prism. Think carefully about the forces that act on the prism as opposed to those on your fingers.

Solution: To add the frictional force on the prism we think about the direction that the prism wants to fall — we know that friction will oppose this motion. Using Newton's third law, the frictional force on our fingers must be equal in magnitude but opposite in direction to that on the prism.

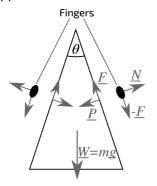


Figure 3: The forces on the isosceles prism and on your fingers as you lift the prism and hold it in static equilibrium. The forces on the right hand side have been labelled, those on the left will have the same magnitudes.

Steps 3 & 4: Concepts, mathematics & symbols

What concepts may we need to solve this problem?

Solution: Newton's first law, Newton's third law and the law of friction.

Write down the magnitude of the frictional force in terms of the coefficient of static friction μ and the normal component, P of the force that you apply to each upper face of the prism.

• Note that the force that you apply to the prism is equal and opposite to the reaction force of the prism on your finger, e.g. $\underline{N} = -\underline{P}$, by Newton's third law.

Solution: From the law of static friction: $F < \mu N = \mu P$

To find the minimum value of P we use the maximum value of F: $F = \mu P$

Apply Newton's First Law vertically.

Solution: From Newton's First Law and resolving forces vertically:

$$2F\cos\left(\theta/2\right)-\left(W+2P\sin\left(\theta/2\right)\right) \ = \ 0$$
 Using $F=\mu P$:
$$2\mu P\cos\left(\theta/2\right)-\left(W+2P\sin\left(\theta/2\right)\right) \ = \ 0$$

By rearranging the latter expression we can write down an expression for the force we apply, P, in terms of μ , the angle θ and the weight of the prism mg.

Solution:

Applied normal force,
$$P = \frac{W}{2 \left[\mu \cos(\theta/2) - \sin(\theta/2) \right]}$$

Step 5: Dimensions & numbers

We are asked to find a force so we should check that the dimensions of our expression are the same as that of a force, $F = [M][L][T]^{-2}$

Solution:

$$\frac{W}{2\left[\mu\cos(\theta/2) - \sin(\theta/2)\right]} = \frac{[\mathsf{M}][\mathsf{L}][\mathsf{T}]^{-2}}{\mathsf{dimensionless quantities}}$$

Our expression is indeed dimensionally correct.

Now using the values given and taking care with the number of significant figures in our answer, m = 100 g, $g = 9.81 \text{ m s}^{-2}$, $\mu = 0.400 \text{ and } \theta = 30.0^{\circ}$.

Solution:

$$P = \frac{W}{2\left[\mu\cos(\theta/2) - \sin(\theta/2)\right]} = \frac{0.100 \times 9.81}{2\left[0.400\cos(15.0) - \sin(15.0)\right]} = 3.85 \,\text{N}$$

Consider whether this is a reasonable answer by comparing it with the weight of an everyday object.

Level 1: Mechanics

Each link by a topic heading will take you to nine more similar problems.

Statics

isaacphysics.org/s/Dbv5Dj

Q: Bed of Nails

A uniform rod of weight $500\,\mathrm{N}$ is supported by two pegs at either end of the rod.

Part A: Draw a free body diagram showing the forces acting on the rod. What is the magnitude of the forces exerted by each of the pegs on the rod?

Part B: If there are now eight pegs evenly spaced along the rod to support its weight, what force is applied by each peg on the rod?

Part C: Using the previous answers, explain how it is possible to lie on a bed of nails, but putting weight on one nail is extremely painful.

Dynamics

isaacphysics.org/s/CMjHTE

Q: A Hamburger

A hamburger has 2.2 MJ of chemical potential energy which can be released by eating it. (Take $g=9.81~{\rm m\,s^{-2}}$)

Part A: How much energy is needed to lift a $50 \, \text{kg}$ student upwards through a height of $0.40 \, \text{m}$?

Part B: How many step-ups of 0.40 m would the student need to make in order to burn off the energy of a hamburger?

Part C: How many hamburgers would the student need to consume in order to reach the top of Mount Everest, a height of $8.8 \, \text{km}$?

Part D: If the energy of a hamburger could be used by itself to propel itself upwards, how high could it rise? (The mass of a hamburger is $0.22 \, \text{kg}$; assume this remains constant. Assume that g also remains constant).

Kinematics

isaacphysics.org/s/IUV78T

Q: A Strange Planet

A lost astronaut lands her spaceship on an unknown planet. She decides to work out the value of the acceleration due to gravity on this planet so that she can check her onboard computer and find out her location. She knows that on Earth (where $g=9.81~{\rm m\,s^{-2}}$ downwards) she takes $1.0~{\rm s}$ to jump up and land again. On this planet, a jump takes $1.4~{\rm s}$.

What is the magnitude of the downward acceleration due to gravity on the strange planet? Assume she can jump up at the same speed on any planet.

Level 2: Mechanics

Statics

isaacphysics.org/s/B16Mzd

Q: Force on Table Legs

A uniform table consists of a circular wooden board of mass $m=3.00\,$ kg resting on top of three vertical legs, each of mass $M=0.500\,$ kg. The legs are equidistant from the centre of the table and form an equilateral triangle. (Take $g=9.81\,$ m s $^{-2}$).

Part A: What is the magnitude of the reaction force from one of the legs on the tabletop?

Part B: What is the magnitude of the reaction force from the ground on one of the legs?

Dynamics

isaacphysics.org/s/4JKSmy

Q: The Lift

A lift, of mass $500 \, \text{kg}$, is travelling downwards at a speed $5.0 \, \text{m s}^{-1}$. It is brought to rest by a constant acceleration over a distance $6.0 \, \text{m}$.

Part A: What is the tension, *T*, in the lift cable when the lift is stopping?

Part B: What is the work done by the tension whilst stopping the lift?

A lift, of mass $500 \, \text{kg}$, is travelling upwards at a speed $5.0 \, \text{m s}^{-1}$. It is brought to rest by a constant acceleration over a distance $6.0 \, \text{m}$.

Part C: What is the tension, *T*, in the lift cable when the lift is stopping?

Part D: What is the work done by the tension whilst stopping the lift?

Kinematics

isaacphysics.org/s/L1TER3

Q: A Stoplight

A car is travelling along a road at constant speed $u=7.00~{\rm m\,s^{-1}}$. The driver sees a stoplight ahead change to amber and applies the brakes. Consequently, the car experiences a total resistive force equal to $\frac{1}{6}$ of its weight and stops just at the stoplight. Taking $g=9.81~{\rm m\,s^{-2}}$, how far does the car travel during the braking period?

Level 3: Mechanics

Statics

isaacphysics.org/s/T2B6VD

Q: Shelf and Brackets

A shelf of uniform density is supported by two brackets at a distance of $\frac{1}{8}$ and $\frac{1}{4}$ of the total length, L, from each end respectively.

Part A: Find the ratio of the reaction forces from the brackets on the shelf. Express your answer in the form of a decimal less than or equal to 1, to three significant figures.

Part B: The rectangular shelf is now replaced with a uniform right-angled triangular shelf (figure given on-line). The centre of mass of a triangle lies at a point $\frac{1}{3}$ of the perpendicular distance from the base to the tip.

Find the new ratio of the forces on the two brackets. Express your answer in the form of a decimal less than 1, to three significant figures.

Dynamics

isaacphysics.org/s/klHQYn

Q: A Moment of Rest

Two bodies, P and Q, of equal mass are travelling towards one another on a level frictionless track, with speeds u and u respectively, where u>v. They make an elastic collision. At some instant during the collision, P is brought instantaneously to rest.

What is the speed, v_Q , of Q at this instant?

Kinematics

isaacphysics.org/s/ktiMKD

Q: The Bolt Thrower

A castle wall has bolt throwers which fire a bolt horizontally at a speed v. In order to fire over the enemy's shields, the bolt must make an angle of at least $\theta=45^\circ$ to the horizontal when it hits the ground. The bolt throwers can be mounted at different heights in the wall and set to fire at different speeds.

Part A: Find the maximum range of a bolt fired from a height $h=10\,\mathrm{m}$.

Part B: Find the speed required to reach the maximum range calculated in Part A.

Level 4: Mechanics

Statics

isaacphysics.org/s/YUWgEx

Q: Spring Triangle

A rod AB of length d=2.00 m is fixed horizontally. Two light identical springs of spring constant k=14.0 N m $^{-1}$ are attached to the rod, one at each end. The loose ends of the springs are attached to each other at a point C and in this framework the springs are just taut. It is found that the angle made by one of the springs to the vertical $\alpha=45.0^{\circ}$. A metal ball is then suspended from the springs at C and the angle made by one of the springs to the vertical is found to be $\beta=30.0^{\circ}$.

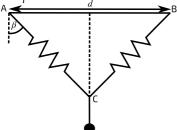


Figure 4: A metal ball suspended from two strings.

Taking the acceleration due to gravity as $g = 9.81 \text{ m s}^{-2}$, what is the mass m of the ball?

(Multiple choice question – see options, concepts and feedback on-line.)

Dynamics

isaacphysics.org/s/4ox4q1

Q: A Ballistic Pendulum

A block of wood with a mass of M=2.5 kg is suspended from fixed pegs by vertical strings l=3.0 m long, in a set up known as a ballistic pendulum. A bullet with a mass of m=10 g and moving horizontally with a velocity u=300 m s⁻¹ enters and remains in the block.

Find the maximum angle θ to the vertical through which the block swings.

Kinematics

isaacphysics.org/s/8BB7Rw

Q: Broken Cannon

A cannon on horizontal ground, at point C, is used to target a point T, $25\,\mathrm{m}$ behind a narrow wall. Unfortunately the cannon is damaged and can only fire at a 45° angle and at one speed. So, the only way to aim the cannon is by moving it towards and away from the target. The gunners aren't sure if they can actually hit the target.

Part A: If the cannonball leaves the cannon at $u=35~{\rm m\,s^{-1}}$; at what distance, d, must the cannon be placed in front of the wall in order to hit the target, if the wall is ignored and the target is at the same height as the cannon?

Part B: The wall is 15 m high. Does the cannonball actually go over the wall and hit the target? If so, by how much?

SHM

isaacphysics.org/s/DZYEBC

Q: Car Suspension over Bumps

The suspension of a car may be considered to be an ideal spring under compression. When the driver, of mass m_1 , steps into the car, of mass m_2 , the vertical height of the car above the road decreases by x. If the car is driven over a series of equally spaced bumps, the amplitude of vibration becomes much larger at one particular speed.

Explain why this occurs, and find an expression for the separation d of the bumps if it occurs at a speed of v.

Angular Motion

isaacphysics.org/s/mcIYvI

Q: Hammer Throwing

At a hammer throwing event, the speed that an athlete is spinning is such that they complete one revolution in $0.50\,\mathrm{s}$. Most of the weight of the hammer is in the ball, so it can be approximated as a point mass $m=7.0\,\mathrm{kg}$ at a distance $l=1.2\,\mathrm{m}$ away from the end of the handle.

The athlete stretches their arms out such that they are holding the end of the handle of the hammer a distance $d=0.60\,\mathrm{m}$ away from their axis of rotation. Assume that the hammer has no vertical motion.

Part A: What is the linear speed of the ball at the end of the hammer?

Part B: What is the kinetic energy of the hammer?

Circular Motion

isaacphysics.org/s/GJMwf0

O: Car on a Roundabout

A car approaches a level roundabout of radius R = 10 m.

Part A: What is the maximum speed that the can travel around the roundabout without slipping, if the coefficient of friction between the road and car is $\mu=0.80$?

A racing car approaches a corner of radius $R=50\,$ m, banked at an angle $\theta=30^\circ$ to the horizontal.

Part B: What is the maximum speed at which the car can travel if it is icy so there is no friction between the wheels and the road?

Part C: What is the maximum speed at which the car can travel around the banked corner and not slip if the road is rough, with coefficient of friction $\mu = 0.55$?

Part D: What is the minimum speed at which the car needs to travel around the banked corner when the road is rough, with coefficient of friction $\mu=0.55$?

Level 4: Fields

Electric Fields

isaacphysics.org/s/q6IUoh

O: Field between Parallel Plates

Two large, parallel metal plates are placed 0.130 m apart. The potential difference between the plates is $150.0\,\mathrm{V}$.

Part A: Electric field strength Calculate the value of the electric field strength between the plates.

Part B: Force on electron Calculate the size of the force on an electron, of charge -1.60×10^{-19} C, placed half way between the plates.

Part C: Force variation How does the force on the electron vary as it moves from the negative plate to the positive plate?

Part D: Potential variation What is the magnitude of the potential difference between two points that are positioned between the parallel plates a distance of $\frac{1}{4}$ and $\frac{3}{4}$ of the way in from one of the plates? Give your answer to 3 significant figures.

Magnetic Fields

isaacphysics.org/s/RjHZfp

Q: Electron in a Magnetic Field

An electron, of charge -1.6×10^{-19} C and velocity 2.35×10^7 m s⁻¹, moves perpendicularly to a magnetic field with magnetic flux density 3.4×10^{-2} T.

Calculate the size of the force on the electron.

Gravitational Fields

isaacphysics.org/s/b9I6Cv

Q: Escaping from the Moon

The mass of the Moon is 7.4×10^{22} kg and its radius is 1.7×10^6 m. Newton's gravitational constant is $G=6.67\times10^{11}$ N m² kg $^{-2}$. Assume a spherical Moon.

Part A: Calculate the gravitational field strength at the Moon's surface.

The mass of the Earth is 6.0×10^{24} kg and its radius is 6.4×10^6 m. Assume that the Earth is spherical.

Part B: What is the escape velocity on the Moon as a fraction of the Earth's escape velocity?

LEVEL 4: FIELDS 17

Gravitational Fields

isaacphysics.org/s/b9I6Cv

Q: Two Orbiting Masses

Two masses of mass m and M are placed with their centres a distance r apart.

Part A: Attractive Force Between Masses Find an expression for the magnitude of the gravitational attractive force between the two masses.

Part B: Centre of Mass In terms of r, how far away from the larger mass M is the centre of mass of the two-mass system?

Part C: Circular Orbit Consider both masses to be performing circular orbits about the centre of mass of the system. Find the speed of the smaller mass in terms of m, M, r and G.

Combined Fields

isaacphysics.org/s/kGlyBR

Q: Where do the Charges Go?

An region of space has an electric field acting to the right and a magnetic field acting "into the screen" as shown in fig. 5.

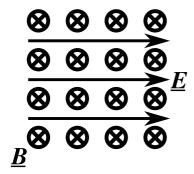


Figure 5: Electric and magnetic fields.

If a single positively charged particle were placed at rest into these fields, in which direction would it move after a short finite time? What direction would a separate negatively charged particle move after a short finite time if it alone were placed at rest into these fields?

(Multiple choice question – see on-line for choices, concepts, hints, video.)

Level 5: Mechanics

Statics

isaacphysics.org/s/ILSBvf

Q: Festival Banner

A festival banner of mass m is to be hung between two buildings of equal height, a distance l apart, by a light inextensible wire of length λl , where λ is a constant. So that it is not stretched, the banner must be placed such that there is equal tension on each length of wire supporting it.

The wire is attached to the roof of the building on the left, and to the side of the building on the right at a height h above the ground. The banner needs to be hung at a distance y vertically below the level of the buildings' roofs, and at a horizontal distance x from the building on the left.

Part A: Length of wire By considering the banner as a point mass, find the length of the wire, λl needed, as a function of l, x, y and h.

Part B: Vertical distance to banner Find y in terms of x and λ .

Part C: Tension in the wire If $\lambda = 2$, find the tension T in the wire.

Dynamics

isaacphysics.org/s/NhtQS1

Q: Picking up a Chain

Part A: Tension in the chain A chain of mass $\lambda=2.0\,\mathrm{kg\,m^{-1}}$ per unit length has a tension T(0) applied to one end. First consider the case where the chain is hanging vertically and is of total length $L=10\,\mathrm{m}$.

Give an expression for the tension and calculate the tension, T(5), at x=5 m, where x=0 is at the upper end of the chain.

Part B: Raising the chain A long length of chain is now placed on a smooth flat surface, and one end is raised at a constant speed $v=5.0\,\mathrm{m\,s^{-1}}$ by a tension T(0).

In the instant that the last piece of chain is raised, i.e.when length, $L=10~{\rm m}$ is suspended, what is T(0)?

Part C: Calculating power What is the power input by T(0) at this point?

Part D: Change in energy What is the rate of change of energy stored in the system as kinetic energy or gravitational potential energy at this point?

Kinematics

isaacphysics.org/s/XarSrv

Q: Crossing a River

A river has banks at x=0 and x=a=20 m, and flows parallel to its banks with a speed u=kx(a-x), where k=0.010 m⁻¹ s⁻¹.

The captain of a ship wishes to moor as far upstream on the opposite bank as possible. If his initial speed is $v=0.50~{\rm m\,s^{-1}}$, what angle θ to the x direction should he set off at? You should assume that the ship's power output is constant, and that it always thrusts in the same direction relative to the banks.

SHM

isaacphysics.org/s/da09Es

Q: Accuracy of an SHM Approximation

A simple pendulum of length L is released from rest from an angle of θ_0 to the vertical. The mass on the end is assumed to be a point mass.

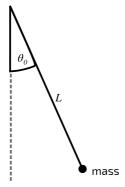


Figure 6: A simple pendulum.

Part A: SHM approximation. Assuming that the pendulum undergoes simple harmonic motion, find an expression for its maximum speed.

Part B: Exact speed. Using conservation of energy, find an exact expression for this speed.

Part C: Compare results. Find the percentage error in the SHM approximation of the maximum speed compared to the true value when $\theta_0 = 0.20$ rad.

Angular Motion

isaacphysics.org/s/HyTNE6

Q: Destroying the Moon

Orbital bombardment is the name for the process where asteroids could be nudged out of their current stable orbit and sent careering into a target. One day a particularly eccentric spaceship captain decides that he doesn't like the Earth's Moon and attempts to destroy it by sending an asteroid to collide with it.

He chooses an asteroid with exactly the same mass as the Moon and alters its orbit so that it will hit the Moon. Only after the asteroid is launched does one of his staff point out that Earth might be in danger as well.

The asteroid collides with the Moon head on, and before the collision it is moving slower than the Moon. The resulting cloud of debris stays together. Ignore the gravitational attraction between the Moon and the asteroid.

Assuming the Moon to be initially in a circular orbit at radius $r=380\,000$ km from the centre of the Earth, using the acceleration of free fall at the Earth's surface $g=9.81\,\mathrm{m\,s^{-2}}$, and given that Earth's radius is R=6378 km, find the maximum speed the asteroid can hit the Moon without the cloud colliding with the Earth

Circular Motion

isaacphysics.org/s/dS3Pg1

O: A Particle in a Bowl

A smooth hemispherical bowl of radius $a=15\,$ cm is placed with its axis of symmetry vertical, and a particle of mass $m=50\,$ g moves in a horizontal circular path on the inside of the bowl with a speed v. The plane of this circle is situated half way down the axis.

Part A: Find the value of v.

Part B: Find an expression for the reaction, N, of the bowl on the particle. What is the magnitude of N?

Level 5: Fields

Electric Fields Q: Inkjet Printing

isaacphysics.org/s/G7rS6I

In some methods of inkjet printing, different droplets are given different amounts of charge as they are fired horizontally out of the nozzle. These droplets are then deflected by different amounts by a deflection voltage that is applied across two electrodes.

In one printer the deflection voltage is $480\,\mathrm{V}$, the length of the deflecting electrodes is $x=1.0\,\mathrm{mm}$ and the distance between them is $d=0.20\,\mathrm{mm}$. The electric field between these electrodes can be assumed to be constant. The droplets produced are approximately spherical with a density of $\rho=1050\,\mathrm{kg\,m^{-3}}$ and a radius of $a=30\,\mathrm{\mu m}$. They leave the nozzle with an initial speed of $u=5.5\,\mathrm{m\,s^{-1}}$.

What is the difference in the magnitude of charge between two droplets that hit the paper at the top and bottom of a letter 'I' of height $h=2.0\,$ mm a distance of $L=0.50\,$ cm away from the edge of the deflecting electrodes? Gravitational effects can be ignored.

Magnetic Fields

isaacphysics.org/s/Nb5XzE

Q: Magnetic Inclination

The Earth's magnetic field is generally not parallel to its surface. Near Cambridge, the magnetic field points downwards at an angle of 66° to the ground. Three particles of equal charges move with the same speed in three different directions: directly towards magnetic North, at right angles to this along the ground (East), and vertically. The Lorentz forces on these particles are labelled as F_{North} , F_{East} and F_{Vertical} respectively.

Order these forces in decreasing magnitude. (Multiple choice question. See choices and feedback on-line.)

Gravitational Fields Q: Estimating Gravity

isaacphysics.org/s/y0Df63

The value for the acceleration due to gravity, $g=9.81\,\mathrm{m\,s^{-2}}$, is only valid near the Earth's surface. Further away from the Earth the value of g varies with the distance from the Earth's surface h.

Part A: Gravity strength at edge of atmosphere. The Earth's atmosphere has a

22 LEVEL 5: FIELDS

thickness of about 700 km. By finding a power series of g in h, estimate the ratio of the acceleration due to gravity at the top of the Earth's atmosphere to that at its surface, given that the radius of the Earth is approximately R=6378 km. You should assume that $h\ll R$ such that $(h/R)^2\approx 0$. Give your answer as $\frac{g_{\rm atmos}}{g_{\rm surface}}$ to 3 significant figures.

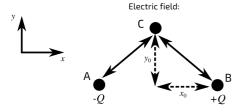
Part B: Estimate error. Estimate the error in your previous answer. Give your answer to 3 significant figures.

Combined Fields

isaacphysics.org/s/rRP40E

Q: Fields in a Triangle

The diagram below shows a triangle ABC in which CA = CB = r. In the first case, an electric field is created by placing point charges -Q and +Q at A and B respectively. In the second, two equal point masses m are situated at A and B to create a gravitational field in the region.



Gravitational field:

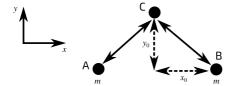


Figure 7: Diagram showing the triangle with electric and gravitational fields.

Part A: Direction of electric field. In which direction, relative to the x- and y-directions, does the resultant electric field at C act? (Multiple choice.)

Part B: Direction of gravitational field. In which direction, relative to the x- and y- directions, does the resultant gravitational field at C act? (Multiple choice.)

Part C: Magnitude of electric field. If $Q=1.60\times 10^{-19}$ C, $x_0=2.0$ mm and $y_0=3.5$ mm, what is the magnitude of the electric field at C?

Part D: Magnitude of gravitational field. If $m=1.0\,\mathrm{kg},\,x_0=2.0\,\mathrm{mm}$ and $y_0=3.5\,\mathrm{mm}$, what is the magnitude of the gravitational field strength at C?

Level 6: Mechanics

Statics

isaacphysics.org/s/i2mLQr

Q: Hanging a Non-uniform Bar

A non-uniform bar of mass m is hung horizontally between two walls, using two light ropes attached to the ends. One of the ropes makes an angle $\theta=36.9^\circ$ to the vertical, and the other makes an angle $\phi=53.1^\circ$ to the vertical.

If the bar is $l=1.00\,$ m long, how far away from the closest edge is the centre of mass?

Dynamics

isaacphysics.org/s/aA2xdL

Q: Space Justice

A police spaceship, of mass $m=10000\,$ kg, travelling at a speed $u=2.00\,$ km s⁻¹ needs to arrest another ship travelling ahead of it at 2.50 km s⁻¹. The police spaceship is capable of splitting itself into two equal parts and supplying them with kinetic energy from a single reserve of 2.00 GJ.

Part A: Calculate the speed of the part of the police spaceship that remains pursuing the other ship. Was the energy reserve sufficient?

Part B: If the reserve is sufficient; how long would it take for the police spaceship to catch the other craft, given that it was initially 3000 km behind?

Kinematics

isaacphysics.org/s/WgAvf5

Q: The Bouncing Ball

A ball is dropped from rest at a height h_0 and bounces from a surface such that the height of the n^{th} bounce, h_n , is given by $h_n=\alpha h_{n-1}$, where h_{n-1} is the height of the previous, $(n-1)^{\text{th}}$ bounce. The factor α has value $0 \le \alpha \le 1$.

Part A: How far does the ball travel before coming to rest, given that $\alpha = 0.25$ and $h_0 = 3.0$ m?

Part B: How long does the ball take to cover this distance?

SHM

isaacphysics.org/s/yV9R96

Q: Gravtube

Imagine a tube had been drilled straight through the centre of a uniform spherical planet. The planet has a radius R and the acceleration due to gravity at its surface is g. An object of mass m is released from rest at one end of the tube. From Gauss's theorem, the gravitational force on an object of mass m inside a uniform massive spherical body (in this case, a planet), is given by $F = -\frac{GMm}{r^2}$ where r is the distance of the small mass from the centre of the planet and M is the mass of the planet that exists inside a sphere of radius r (ie. all the mass of the planet that is closer to the planet's centre than the mass m). The force is negative as it acts inwards, towards the point r=0.

Show that the acceleration of an object inside this tube is of the form $a=-\omega^2 r$ and so the object moves with simple harmonic motion.

Part A: What is the time period of the resulting oscillation if $g = 6.00 \text{ m s}^{-2}$, and R = 1200 km?

A satellite is placed in a circular orbit around the same planet, so that it is orbiting just above the ground (ie, at a radius R). The centripetal acceleration of an object of mass m, in a circular orbit at a radius r, is given by $a_c = \omega^2 r$, where ω is the angular velocity of the mass in orbit.

Part B: Find an expression for ω and calculate the time period of the orbit at this radius?

Angular Motion Q: Rising Hoop

isaacphysics.org/s/4k2no4

Two beads, each of mass m, are positioned at the top of a frictionless hoop of mass M and radius R, which stands vertically on the ground. The beads are released and slide down opposite sides of the hoop.

What is the smallest value of $\frac{m}{M}$ for which the hoop will rise up off the ground at some time during the motion?