

Instability in Geophysical Flows

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Errata

- Page 28, equations following (2.15) are missing a factor ν . They should read

$$\vec{\nabla} \cdot \frac{\partial \vec{u}'}{\partial t} = -\vec{\nabla} \cdot \vec{\nabla} \pi' + \vec{\nabla} \cdot (b' \hat{e}^{(z)}) + \nu \vec{\nabla} \cdot \nabla^2 \vec{u}',$$

or,

$$\frac{\partial}{\partial t} \underbrace{(\vec{\nabla} \cdot \vec{u}')}_{=0} = -\nabla^2 \pi' + \frac{\partial b'}{\partial z} + \nu \nabla^2 \underbrace{(\vec{\nabla} \cdot \vec{u}')}_{=0}.$$

- Page 46, reference following (2.61) is to Figure 2.10 (not 2.11).
- Page 70, first equation for $\vec{U} \cdot \vec{A}$ should read

$$\vec{U} \cdot \vec{A} = \begin{bmatrix} U_1 A_{11} & U_1 A_{12} & U_1 A_{13} \\ U_2 A_{21} & U_2 A_{22} & U_2 A_{23} \\ U_3 A_{31} & U_3 A_{32} & U_3 A_{33} \end{bmatrix}.$$

- Page 100 on line preceding (3.86): reference is to Figure 3.21 (not 3.20).
- Page 118: The equation at the bottom of the page is missing a factor of 2. It should read

$$c = \pm \sqrt{\frac{\Delta b}{2k} - \frac{\Delta u^2}{4}},$$

and the accompanying equation at the top of page 119 should therefore read

$$\sigma = \pm \sqrt{\frac{\Delta u^2}{4} k^2 - \frac{\Delta b}{2} k}.$$

The nondimensional variables that follow can be redefined as

$$c^* = \frac{c}{\Delta u}; \quad k^* = k \frac{2\Delta u^2}{\Delta b}; \quad \sigma^* = \frac{2\Delta u}{\Delta b} \sigma$$

in which case the remaining expressions in the subsection are correct.

- Figure 4.8: The final sentence of the caption should read “The scaled wavenumber and growth rate are defined as $k^* = 2k\Delta u^2/\Delta b$ and $\sigma^* = 2\sigma\Delta u/\Delta b$, respectively.”
- Page 158, line 3: “roundoff error” should read “truncation error”.
- Page 174, equation (7.4) should read

$$\frac{Dw}{Dt} = -\frac{\partial \pi}{\partial r}$$

- Page 179, first unnumbered equation should read

$$\frac{d\hat{\psi}}{dr} = -\frac{\ell}{r}\hat{\psi}.$$

- Page 193, definition preceding (7.42) should read

$$\hat{u} = -\imath m \hat{\psi}(r); \quad \hat{w} = \frac{1}{r} \frac{d}{dr} r \hat{\psi}(r),$$

and (7.42) itself should read

$$\frac{d}{dr} \left[\frac{1}{r} \frac{d}{dr} (r \hat{\psi}) \right] + \left[\frac{\Phi}{(W-c)^2} - \frac{Z}{W-c} - m^2 \right] \hat{\psi} = 0,$$

- Page 243, last paragraph of 10.1.2, line 2: superfluous word “that”.
- Page 300, following first sentence, add: “If the fastest-growing mode is found at the limit $k \rightarrow \infty$, just use your largest value of k .”
- Page 302: Exercise 18 should be accompanied by an extra copy of figure 8.6 for the student to draw on.
- Page 313: Project B.2 should include a numerical solution of (B.29).