Black-Scholes Model Errata

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page 8, line -4

Replace

$$u_t(t,z) = -\frac{1}{2}\sigma^2 x^2 u_{zz}(t,z) - rzu_x(t,z) + ru(t,z) \quad \text{for } 0 < t < T, \ z \in \mathbb{R}.$$

by

$$u_t(t,z) = -\frac{1}{2}\sigma^2 z^2 u_{zz}(t,z) - rzu_z(t,z) + ru(t,z) \quad \text{for } 0 < t < T, \ z \in \mathbb{R}.$$

page 19, line -10

Replace

Defintion 2.11

We say that (x(t), y(t)) is an **arbitrage opportunity** (or simply an arbitrage) if $V_{(x,y)}(0) = 0$, $V_{(x,y)}(t) \ge -L$, for all *t* and some constant *L*, and with positive probability $V_{(x,y)}(t') > 0$ for some *t'*.

by

Definition 2.11

We say that a self-financing strategy (x(t), y(t)) is an **arbitrage opportunity** (or simply an arbitrage) if

1. $V_{(x,y)}(0) = 0$,

2. $V_{(x,y)}(t) \ge -L$, for all *t* and some constant *L*,

3. for some t', $V_{(x,y)}(t') \ge 0$ and with positive probability $V_{(x,y)}(t') > 0$.

page 20, line 14

Replace

Definiton 2.13

We say that (x(t), y(t), z(t)) is an **arbitrage** (in the extended market) if $V_{(x,y,z)}(0) = 0$, $V_{(x,y,z)}(t) \ge -L$, for all *t* and some constant *L*, and with positive probability $V_{(x,y,z)}(t') > 0$ for some *t'*.

1

Definiton 2.13

We say that a self-financing strategy (x(t), y(t), z(t)) is an **arbitrage** (in the extended market) if

1. $V_{(x,y,z)}(0) = 0$, 2. $V_{(x,y,z)}(t) \ge -L$, for all *t* and some constant *L*, 3. for some *t'*, $V_{(x,y,z)}(t') \ge 0$ and with positive probability $V_{(x,y,z)}(t') > 0$.

page 55, line 9

Replace

$$= \mathbb{E}_{\mathcal{Q}}(\mathrm{e}^{-r(T-t)}K\mathbf{1}_{\{S(T)\leq K\}}|\mathcal{F}_t) - \mathbb{E}_{\mathcal{Q}}(\mathrm{e}^{-r(T-t)}S(T)\mathbf{1}_{\{S(T)-K\}}|\mathcal{F}_t)$$

by

$$= \mathbb{E}_{\mathcal{Q}}(\mathrm{e}^{-r(T-t)}K\mathbf{1}_{\{S(T) \leq K\}} | \mathcal{F}_t) - \mathbb{E}_{\mathcal{Q}}(\mathrm{e}^{-r(T-t)}S(T)\mathbf{1}_{\{S(T) \leq K\}} | \mathcal{F}_t)$$

page 66, line -4 Replace: $S(t + u) = x + \sigma W(u)$

by: $S(t + s) = x + \sigma W(s)$

page 66, line -2

Replace: s < Tby: t < T

page 67, line 1

Replace:

Then $u(t, x + \sigma W(T - t))$ is a martingale and

by:

Then $u(s, x + \sigma W(s - t))$ is a martingale for $s \in [t, T]$, and

page 67, line 7

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Replace:
genereal
by:
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general

page 124, line 14

2 by

3

Replace

$$u_t + rxu_z + \frac{1}{2}\sigma^2 z^2 u_{zz} = ru$$

by:

$$u_t + rzu_z + \frac{1}{2}\sigma^2 z^2 u_{zz} = ru$$

page 145, line 3 Replace:

$$=\exp\{-\frac{1}{2}\frac{(\mu-r)^2}{c_1^2+c_2^2}T-(\mu-r)\frac{c_1}{c_1^2+c_2^2}W_1(t)+(\mu-r)\frac{c_2}{c_1^2+c_2^2}W_2(t)\}.$$

by

$$= \exp\{-\frac{1}{2}\frac{(\mu-r)^2}{c_1^2+c_2^2}T - (\mu-r)\frac{c_1}{\sqrt{c_1^2+c_2^2}}W_1(t) + (\mu-r)\frac{c_2}{\sqrt{c_1^2+c_2^2}}W_2(t)\}.$$

page 148, line 11

Replace

$$S_{i}(t) = S_{i}(0) \exp\{\int_{0}^{t} \mu_{i}(t)dt - \frac{1}{2}\sum_{j,l=1}^{d}\int_{0}^{t} \sigma_{ij}^{2}(t)dt + \sum_{j=1}^{d}\int_{0}^{t} \sigma_{ij}(t)dW_{j}(t)\}$$

by

$$S_{i}(t) = S_{i}(0) \exp\{\int_{0}^{t} \mu_{i}(s)ds - \frac{1}{2}\sum_{j,l=1}^{d}\int_{0}^{t} \sigma_{ij}(s)\sigma_{lj}(s)ds + \sum_{j=1}^{d}\int_{0}^{t} \sigma_{ij}(s)dW_{j}(s)\}$$

page 150, lines 3-7 Replace *dt* by *ds* (twice)

page 153, line -8 Replace

$$[Y_1, Y_2](t) = \int_0^t (b_{11}(s)b_{21}(s) + b_{12}(s)b_{22}(s)) \, ds.$$

$$[Y_1, Y_2](t) = \int_0^t (b_{11}(s)b_{12}(s) + b_{21}(s)b_{22}(s)) \, ds.$$

page 165, line -4 Replace: $Y(t) = \frac{S_2(T)}{S_1(T)}$ by: $Y(T) = \frac{S_2(T)}{S_1(T)}$

4 by