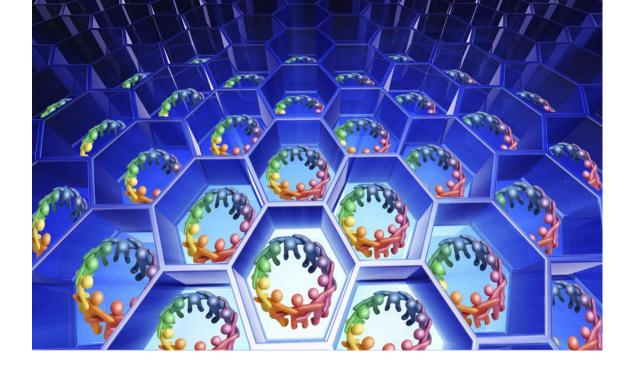
Cooperative Communications and Networking

Chapter 17

**Broadband Cooperative Communications** 



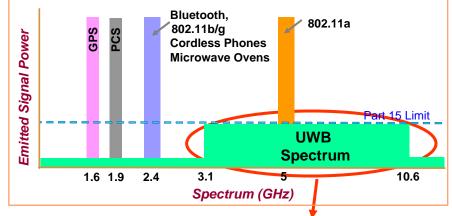
# Outline

- Introduction and motivations
- System model
- Cooperative Protocol and Relay Assignment Scheme
- Performance analysis
- Optimum Relay Location
- Simulation results
- Conclusions

# Introduction

Ultra-wideband (UWB) offers a great potential for the design of high-speed wireless personal area networks





- Transmitted power level is limited to allow coexistence with other systems
- In broadband communications, OFDM is an effective means to improve performance

#### Motivations

Challenge: With the limited transmit power level, how to achieve the desired performance and coverage range?



 To improve performance in broadband systems, the fundamental concept of diversity can be applied.

In this chapter, we study an OFDM cooperative protocol that improves performance based on fixed relaying protocol. • Limited feedback

 Practical relay assignment

# System Model

- OFDM Wireless Network i.e. WLAN or WPAN
- Circular cell of radius  $\rho$
- A central node and multiple users, each communicating with the central node
- K users, uniformly located within the cell
- The user's distance  $D_{s,d}$
- Uplink scenario  $p_{D_{s,d}}(D) = 2D / \rho^2$ ,  $0 \le D \le \rho$
- Data packet consists of: preamable, header, and frame payload
- The fade is modeled as zero mean, complex Gaussian random variable
- The channel impulse response from node i to node j can be modeled as:

delay

$$\boldsymbol{h}_{i,j}(\boldsymbol{t}) = \sum_{l=0}^{L} \boldsymbol{\alpha}_{i,j}(l) \boldsymbol{\delta}(\boldsymbol{t} - \boldsymbol{\tau}_{i,j}(l))$$

### System Model

• Consider OFDM with N subcarriers, then we can express the channel frequency response as:

$$H_{s,d}(n) = \sum_{l=0}^{L-1} \alpha_{s,d}(l) \exp(-j2\pi n \tau_{s,d}(l)/N)$$

• The received signal at subcarrier *n* of destination *d* from source user *s* can be modeled as:

$$y_{s,d}(n) = \sqrt{P_{nc} \kappa D^{-v}_{s,d}} H_{s,d}(n) x_s(n) + z_{s,d}(n)$$

- $P_{nc}$  is the transmitted power  $N_0$
- $x_s(n)$  denotes an information symbol
- $z_{s,d}(n)$  is an additive white Gaussian noise with zero mean and variance

### System Model

• Let each information symbol have unit energy. For a given distance between source and destination, the received signal-to-noise ratio SNR for the *n*-th subcarrier can be given by:

$$\zeta_{s,d}^{(n)} = P_{nc} \kappa D_{s,d}^{-\nu} |H_{s,d}(n)|^2 / N_0$$

• In case of direct transmission between two nodes the are D, apart the maximum average mutual information in a subcarrier *n* is:

$$I^{(n)}(D_{s,d}) = \log(1 + \zeta_{s,d}^{(n)})$$

• Let R denote a rate for each subcarrier, then the probability that a subcarrier is in outage can be given by

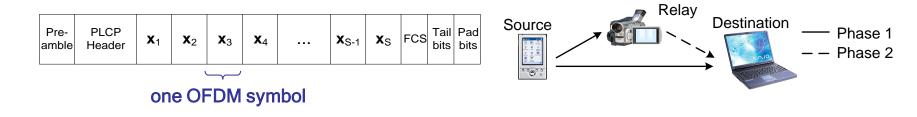
$$P_{out}^{D}(D_{s,d}) = \Pr(I^{(n)}(D_{s,d}) \le R) = \Pr(\zeta_{s,d}^{(n)} \le 2^{R} - 1)$$

• Phase 1: Each user transmits its packet to the destination (central node) and the packets are also received at the delay

• The destination performs channel estimation using the OFDM pilot symbols, then broadcasts the indices of the subcarriers whose symbols are not received successfully.

• Phase 2: The relay decodes the source symbols that are unsuccessfully received at the destination via direct transmission, then forwards the decoded information to the destination.

• The protocol makes efficient use of the available bandwidth by allowing the relay to forward the information of multiple sources in one OFDM block

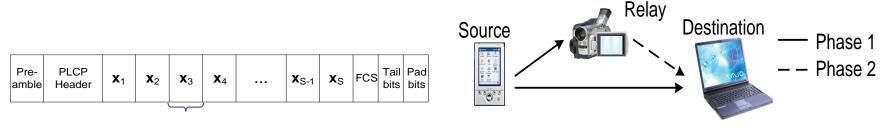


• Assume a relay is assigned to help k users,

• In phase 2, how will the destination know which relay subcarriers carry information of which users?

• Additional overhead vs. Fixed relay assignment scheme

• Fixed relay assignment scheme: if  $n_i$  subcarriers of user *i* are in outage, then in phase 2, the relay can use the first  $n_1$  subcarriers to transmit the data of user 1 and so on.



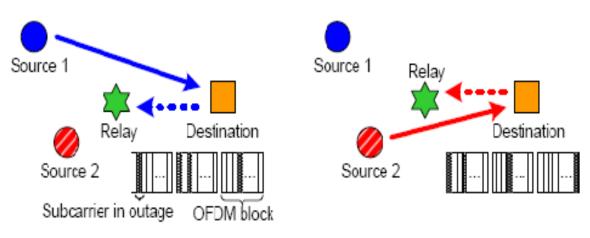
one OFDM symbol

• In phase 1, the received signals at the destination and the relay are

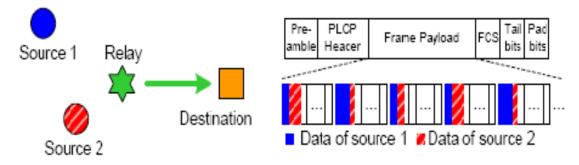
$$y_{s,d}(n) = \sqrt{P_c \kappa D_{s,d}^{-\nu}} H_{s,d}(n) x_s(n) + z_{s,d}(n)$$
$$y_{s,r}(n) = \sqrt{P_c \kappa D_{s,r}^{-\nu}} H_{s,r}(n) x_s(n) + z_{s,r}(n)$$

• In phase 2, the signal received at the destination from the relay is

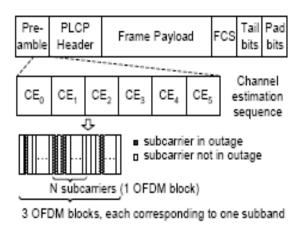
$$y_{r,d}(n) = \sqrt{P_c \kappa D_{r,d}^{-\nu} H_{r,d}(n) \widetilde{x}_s(n)} + z_{r,d}(n)$$

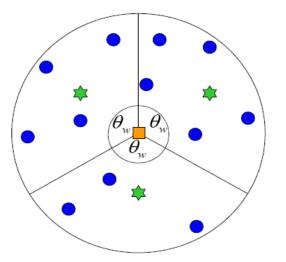


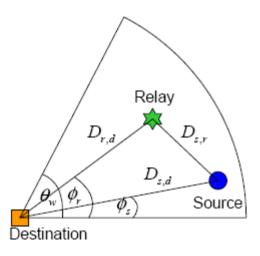
(a) Phase 1: Source transmits information to the destination



(b) Phase 2: Relay forwards source information to the destination







An example of relay assignment for a multi-user OFDM system: a cell with three relays

Let W denote the number of relays in a circular cell. The relay assignment is as follows:

• The cell is equally divided into W sectors, each with a central angle  $2\pi/W$ 

• One relay is assigned to help users within each sector

• In each sector, the relay is placed at an optimum relay location which minimizes the outage probability for all possible source-destination pairs

• Outage probability in non-cooperative mode: channel resources (time and frequency) divided among K users

$$P_{out}^{D}(D_{s,d}) = \Pr(I^{(n)}(D_{s,d}) \le R) = \Pr(\zeta_{s,d}^{(n)} \le 2^{R} - 1)$$

• In cooperative mode, the same channel resources are divided among K + W users, thus the mutual information in each subcarrier is given by

$$K/(K+W)I^{(n)}(D_{i,j})$$

• which corresponds to the event

$$|H_{i,j}(n)|^{2} \leq \frac{(2^{(K+W)R/K} - 1)N_{0}}{\kappa P_{c}} D_{i,j}^{-\nu} \cong \beta D_{i,j}^{-\nu}$$

• Under the described protocol, the average probability that a subcarrier is in outage can be expressed as

$$P_{out} = \sum_{k=0}^{K} P_{out|k} \operatorname{Pr}(k \text{ users in the sector})$$

• Where  $P_{out|k}$  denotes the outage probability per subcarrier given k users are in the sector

Pr(k users in the sector) = 
$$\binom{K}{k} \left(\frac{1}{W}\right)^k \left(1 - \frac{1}{W}\right)^{K-k} = c(k)$$

•  $P_{outk}$  can be determined as follows. In the case the relay has available resources to help forward the source information, the outage event in subcarrier *n* is equivalent to the event

$$\Phi = (\{I^{(n)}(D_{s,d}) \leq \widetilde{R}\} \cap \{I^{(n)}(D_{s,r}) \leq \widetilde{R}\}) \cup (\{I^{(n)}(D_{s,d}) \leq \widetilde{R}\})$$
$$\cap \{I^{(n)}(D_{r,d}) \leq \widetilde{R}\} \cap \{I^{(n)}(D_{s,r}) > \widetilde{R}\})$$

•  $\widetilde{R} = (K+W)R/K$  Note, the events in the union are mutually exclusive

$$\Pr(\{I^{(n)}(D_{i,j}) \le \widetilde{R}\}) = \Pr(|H_{i,j}(n)|^{2} \le \beta D_{i,j}^{\nu}) = 1 - \exp(-\beta D_{i,j}^{\nu})$$

$$P_{out}^{C} = \left[1 - \exp\left(-\frac{(2^{\widetilde{R}} - 1)N_{0}D_{s,d}^{\nu}}{\kappa P_{c}}\right)\right] \left[1 - \exp\left(-\frac{(2^{\widetilde{R}} - 1)N_{0}}{\kappa P_{c}}(D_{s,r}^{\nu} + D_{r,d}^{\nu})\right)\right]$$

$$P_{out}^{D} = \Pr(I^{(n)}(D_{s,d}) \le \widetilde{R}) = 1 - \exp\left(-\frac{(2^{\widetilde{R}} - 1)N_{0}D_{s,d}^{\nu}}{\kappa P_{c}}\right)$$

$$P_{out}^{D} = \Pr(I^{(n)}(D_{s,d}) \le \widetilde{R}) = 1 - \exp\left(-\frac{(2^{\widetilde{R}} - 1)N_{0}D_{s,d}^{\nu}}{\kappa P_{c}}\right)$$

•  $Q|_k$  is defined as the probability that a source subcarrier that is in outage is not helped by the relay

•  $Q|_k$  can be determined as follows. Consider a sector with *k* users, each transmitting information in *N* subcarriers during one OFDM symbol period.

• The total number of kN subcarriers (in k OFDM symbol periods) are used to transmit information from all k users in the sector.

• Given that x out of kN subcarriers in outage, the probability that a subcarrier in outage is not helped by the relay is (x-N)/x for  $N+1 \le x \le kN$ 

$$Q|_{k} = \sum_{x=N+1}^{kN} \frac{x-N}{x} \Pr(x \text{ out of } kN \text{ subcarriers in outage})$$

 $\Pr(x \text{ out of } kN \text{ subcarriers in outage}) = \binom{kN}{x} \left(P_{out}^{D}\right)^{x} \left(1 - P_{out}^{D}\right)^{kN-x}$ 

$$P_{out} = (1 - \exp(-\beta D_{s,d}^{v})) \left[ 1 - \exp(-\beta (D_{s,r}^{v} + D_{r,d}^{v})) (1 - g(D_{s,d})) \right]$$
$$g(D_{s,d}) = \sum_{k=1}^{K} c(k) Q|_{k}$$

• The average outage probability can be determined by averaging over the distribution of the user's distance. We assume the users are uniformly distributed within the cell.

$$p_{D}(D \mid 0 \le \phi_{s} \le \phi_{W}) = \frac{2D}{W\rho^{2}}, 0 \le D \le \rho$$

$$\overline{P}_{out} = \frac{1}{\pi\rho^{2}} \int_{0}^{\rho} \int_{0}^{\frac{2\pi}{W}} \left[ 1 - e^{-\beta(f^{v}(D_{s,d},\phi_{s}) + D_{r,d}^{v})} (1 - g(D_{s,d})) \right] \times D_{s,d} (1 - e^{-\beta D_{s,d}^{v}}) d\phi_{s} dD_{s,d}$$

[17]

• Use Genie-Aided relay assignment scheme to find lower bound.

• Optimum distance between the relay and the destination

$$D_{s,r} = D_{s,d} - D_{r,d}$$

• The optimum relay location for a source-destination pair can be obtained by solving

$$D_{r,d}^{*} = \arg \min_{D_{r,d}} \{1 - \exp(-\beta((D_{s,d} - D_{r,d})^{v} + D_{r,d}^{v}))(1 - g(D_{s,d}))\} s.t.0 \le D_{r,d} \le D_{s,d}$$

$$D_{r,d}^{*} = D_{s,d} / 2$$
• By substitution  $D_{r,d}^{*} = D_{s,d} / 2$ 

$$D_{s,r}^{*} = D_{s,d} - D_{r,d}^{*} = D_{s,d} / 2$$

$$P_{out} \ge (1 - \exp(-\beta D_{s,d}^{v})) \Big[ 1 - (-\beta D_{s,d}^{v} / (2^{v-1}))(1 - g(D_{s,d})) \Big]$$

# **Optimum Relay Location**

- Based on the average outage probability
- Users are uniformly located in the cell

• Optimum relay location is the line that divides the central angle into two equal parts

$$\phi_r^* = \theta_w / 2$$

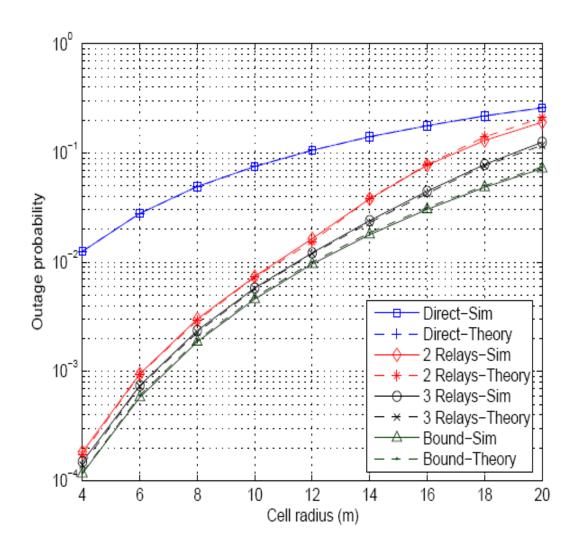
- Next find the optimum relay distance
- Take the first derivative of  $\overline{P}_{out}$  with respect to  $D_{r,d}$

• Approximate location can be shown to be

$$\overline{D}_{r,d} = \overline{D}_{s,d} / 2$$

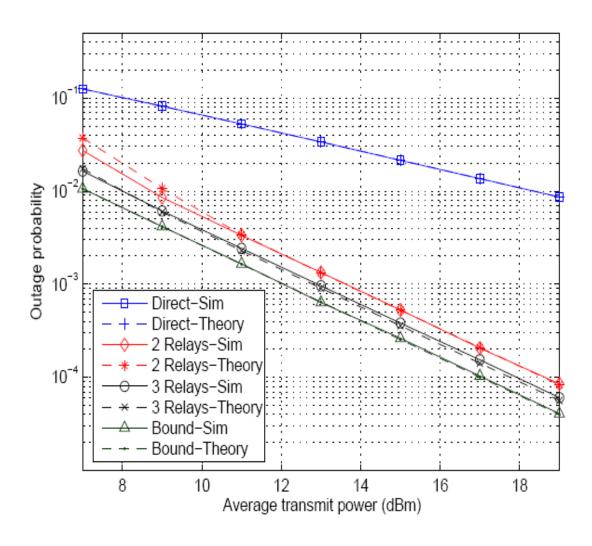
### Simulation and Results

- WLAN scenario
- 64 subcarriers
- R = 1 bit/s/Hz per user
- I0 users



## Simulation and Results

- WLAN scenario
- 64 subcarriers
- R = 1 bit/s/Hz per user
- 10 users



#### Conclusions

- Bandwidth efficient protocol for multi-user OFDM systems
- Destination broadcasts subcarrier indices that are in outage
- Relay forwards only the source symbols in those subcarriers
- Data of multiple sources in one OFDM symbol
- Relay assignment algorithm described
- Optimum relay location determined